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# Sequential Charmonium Suppression

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# 1. Charmonium Binding and Dissociation

Charmonia:  $c\bar{c}$  bound states stable under strong decay

Binding energy  $\Delta E = 2 M_D - M_i$

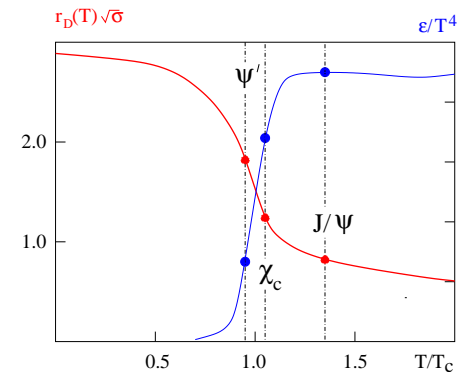
ground state  $J/\psi$ : tightly bound  $\Delta E \gg \Lambda_{QCD}$ , very small  $r_{J/\psi} \ll r_h$

What happens to binding in QGP?

Colour screening  $\Rightarrow$  binding becomes **weaker** and of **shorter range**

What happens when  
**force range** < **charmonium radius**?

$Q$  and  $\bar{Q}$  cannot “see” each other  
 $\Rightarrow$  charmonium **dissociates**



⇒ charmonium dissociation points determine temperature, energy density of medium

How to calculate? Three possibilities:

1. model heavy quark potential  $V(r, T)$ , solve Schrödinger equation:

Karsch et al. 1988, Digal et al. 2001

$$T_{J/\psi} \gtrsim T_c, T_\chi \text{ \& } T_{\psi'} \lesssim T_c$$

2. determine heavy quark potential  $V(r, T)$  in lattice QCD, solve Schrödinger equation

Wong 2004, 2005

Alberico et al. 2005

Digal et al. 2005

state	$J/\psi(1S)$	$\chi_c(1P)$	$\psi'(2S)$
$T_d/T_c$	2.10	1.16	1.12

3. calculate quarkonium spectrum directly in finite  $T$  lattice QCD

quenched: Umeda et al. 2001, Asakawa & Hatsuda 2004, Datta et al. 2004, Iida et al. 2005

unquenched: Morrin et al. 2005

state	$J/\psi(1S)$	$\chi_c(1P)$	$\psi'(2S)$
$T_d/T_c$	> 2.0	< 1.1	?

Conclude:

- $J/\psi$  survives up to  $T \geq 2 T_c \Rightarrow \epsilon_{J/\psi} \geq 15 \text{ GeV}/\text{fm}^3$
- $\chi_c$  and  $\psi'$  dissociated near  $T_c \Rightarrow \epsilon_{\psi',\chi} \simeq 0.5 - 2 \text{ GeV}/\text{fm}^3$
- caveats: thermal activation, widths as  $f(T)$

Schematic Approach:

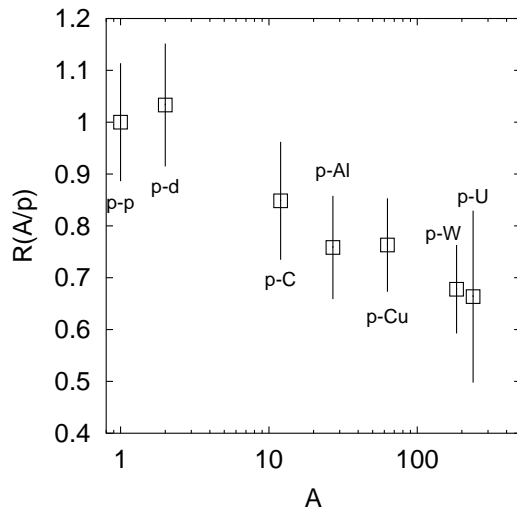
- $\psi'$  and  $\chi_c$  melt at same point  $T \simeq T_c$ ,  
same suppression pattern  $S_{\psi'}(T) \simeq S_{\chi}(T)$
- $J/\psi$  survives up to much higher  $T_{J/\psi} \gg T_c$ ,  
so that for  $T \leq 2T_c$ ,  $S_{J/\psi}(T) = 1$ .
- in hadronic collisions, 60%  $J/\psi$  are directly produced  $1S$  states,  
30% come from  $\chi_c$  decay, 10% from  $\psi'$  decay.
- hence

$$S_{J/\psi}(T) = 0.4 S_{\psi'}(T) + 0.6 \quad \forall T \leq 2T_c$$

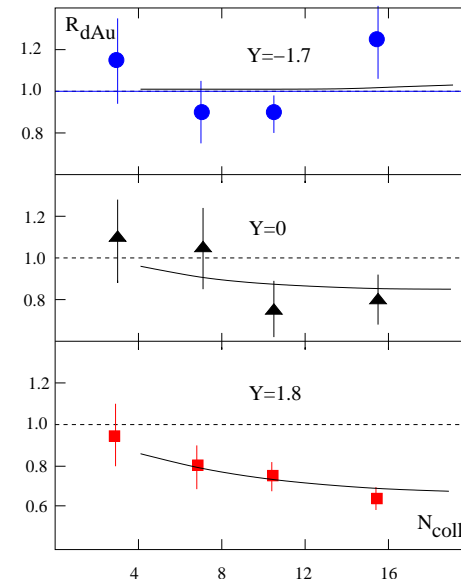
$\Rightarrow$  scaling relation for data.

## 2. Charmonium Production in Nuclear Collisions

To probe produced medium, account for effects of nuclear medium  
determine normal nuclear absorption through  $p-A$  or  $d-A$  studies



nuclear suppression at SPS ( $p - A$ )



at RHIC ( $d - Au$ )

specify dissociation cross sections  $S \sim \exp\{-n_0 \sigma_i L\}$

(SPS full Glauber analysis)

**SPS**

$$\sigma_{J/\psi} = 4.18 \pm 0.35 \text{ mb}$$

$$\sigma_{\psi'} = 7.3 \pm 1.6 \text{ mb}$$

**RHIC**

$$\sigma_{J/\psi}(y = 1.8) = 3.1 \pm 0.2 \text{ mb}$$

$$\sigma_{J/\psi}(y = 0) = 1.2 \pm 0.4 \text{ mb}$$

$$\sigma_{J/\psi}(y = -1.7) = -0.1 \pm 0.2 \text{ mb}$$

use to account for normal nuclear absorption in  $AA$  collisions

• SPS:

calculate  $(d\sigma_i/dy)_{Gl}$  as function of centrality, then define

survival probability 
$$S_i = \frac{(d\sigma_i/dy)_{ex}}{(d\sigma_i/dy)_{Gl}}$$

for  $i = J/\psi, \psi'$  in  $AA$  collisions as function of centrality

- RHIC:

experiment provides  $J/\psi$  production rates in  $AuAu$  collisions relative

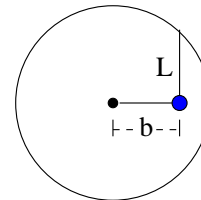
to  $pp$  collisions  $R_{AuAu}(y, N_{part})$

as function of rapidity  $y$  and centrality  $N_{part}$

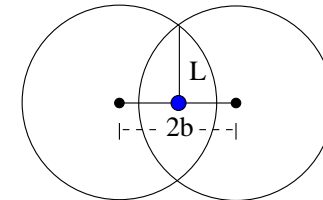
define survival probability

$$S(y, N_{part}) = \frac{R_{AuAu}(y, N_{part})}{\{exp\{-n_0[\sigma_{diss}(y) + \sigma_{diss}(-y)]L\}}$$

centrality measures  $b$ ,  $L$ ,  $N_{part}$ ,  $\epsilon$   
related by Glauber



p-A



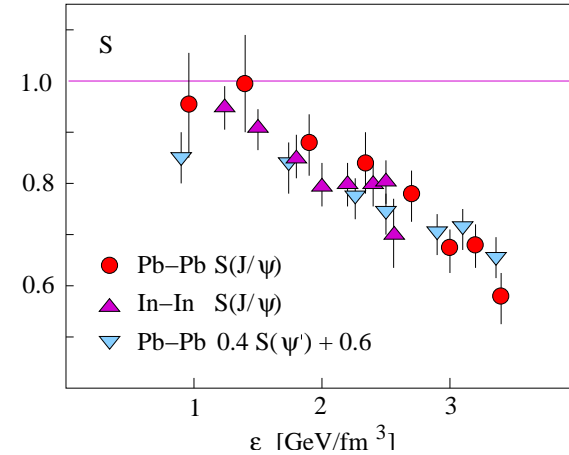
A-A

### 3. Analysis of Nuclear Collision Results

- scaling relation for  $\psi'$  and  $J/\psi$

$$S_{J/\psi}(T) = 0.4 S_{\psi'}(T) + 0.6 \quad \forall T \leq 2T_c$$

in reasonable accord with SPS data

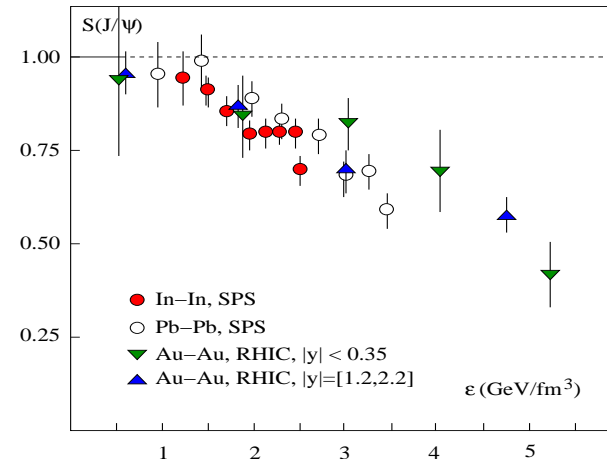


- constant  $J/\psi$  rate  $S_{J/\psi} \simeq 0.6$

beyond  $\psi'$ ,  $\chi_c$  suppression region

in reasonable accord with

combined RHIC/SPS data

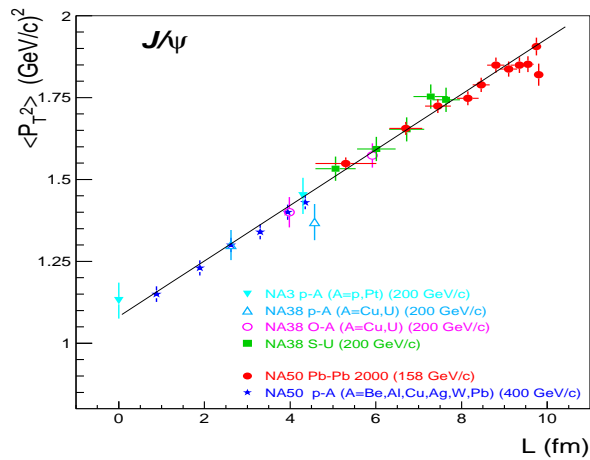
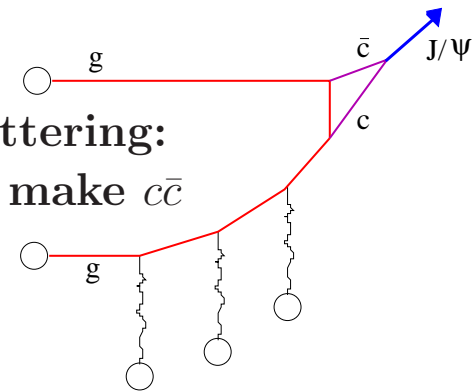




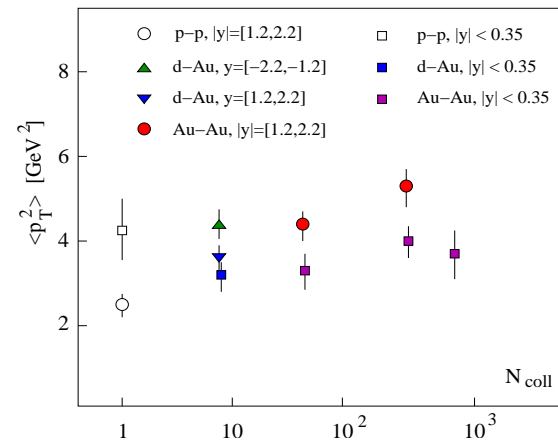
- $J/\psi$  transverse momentum behaviour

$p_T$ -broadening due to initial state parton scattering:  
gluons scatter several times before fusing to make  $c\bar{c}$

$\Rightarrow \langle p_T^2 \rangle$  increases  
with  $A$  in  $p-A$ , with centrality in  $A-A$



SPS



RHIC

random walk of projectile gluon  $\Rightarrow p - A$ :

$$\langle p_T^2 \rangle_{pA} = \langle p_T^2 \rangle_{pp} + N_c^A \delta_0$$

$\exists N_c^A + 1$  pre-fusion collisions of incident projectile gluon in target  
and each subsequent collision gives “kick”  $\delta(s)$

random walk of pre-fusion projectile and target gluons  $\Rightarrow A - A$ :

$$\langle p_T^2 \rangle_{AA} = \langle p_T^2 \rangle_{pp} + N_c^{AA} \delta_0$$

with  $N_c^{AA}$  sum of subsequent collisions of projectile gluon in target  
plus those of target gluon in projectile

calculate  $N_c^A$  via Glauber, determine  $\delta(s)$  from  $p - A$

calculate  $N_c^{AA}$  via Glauber, predict  $\langle p_T^2 \rangle_{AA}$ , IF no new  $A - A$  effects

## Calculation of $N_c^A$

number of collisions of projectile nucleon in target

$$N_c = (3/4) 2 R_A n_0 \sigma$$

with  $\sigma(s) \sim$  nucleon-nucleon cross section

if average fusion at center of target,  $N_c^A \simeq (N_c - 1)/2$

normal nuclear absorption shifts fusion point “down-stream”,

up to maximum  $N_c^A \simeq (N_c - 1)$ ; estimate (K-N-S) gives  $N_c^A \simeq 3 \pm 1$

**SPS:**

$$\langle p_T^2 \rangle_{pU} = 1.49 \pm 0.05 \text{ GeV}^2 - \langle p_T^2 \rangle_{pp} = 1.25 \pm 0.05 \text{ GeV}^2 \Rightarrow \delta \simeq 0.05 \text{ GeV}^2$$

**RHIC:**

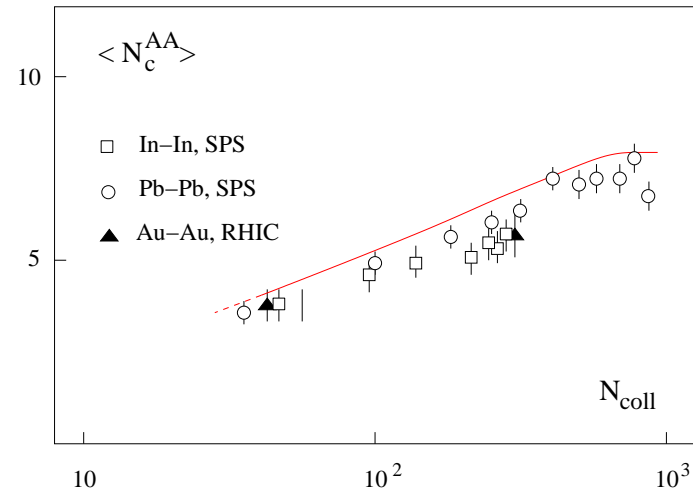
$$\langle p_T^2 \rangle_{pp} = 2.51 \pm 0.21 \text{ GeV}^2 - \langle p_T^2 \rangle_{dAu} = 3.96 \pm 0.28 \text{ GeV}^2 \Rightarrow \delta \simeq 0.3 \text{ GeV}^2$$

- with  $N_c^A$  and  $\delta(s)$  given\*,

further scaling relation

$$N_c^{AA}(SPS) \simeq N_c^{AA}(RHIC)$$

as function of centrality




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\* different value of  $N_c^A$  only shifts scale of  $N_c^{AA}$

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transverse momentum dynamics same at RHIC and SPS,  
only kick  $\delta(s)$  differs

broadening correctly reproduced by Glauber based on

- initial state parton scattering
- normal nuclear absorption

no evidence for new behaviour

(direct  $J/\psi$  suppression,  $J/\psi$  formation by recombination)

## Conclusions

SPS (Pb-Pb, In-In) and RHIC (Au-Au) data indicate

- onset of  $\psi' \sim \chi_c$  suppression around  $\epsilon \simeq 1 - 1.5 \text{ GeV/fm}^3$
- approximately constant  $S_{J/\psi} \simeq 0.6$  above that  
(no significant direct  $J/\psi$  suppression)

Agrees with present knowledge of in-medium  $J/\psi$  behaviour  
in finite temperature QCD

Further Tests:

more precise  $\psi'$  data (NA60)

direct  $\chi_c$  data (?)

onset of direct  $J/\psi$  suppression (LHC)

NB: recombination  $\rightarrow$  onset of  $J/\psi$  enhancement