

Im?Perfect Fluidity in Pb+Pb at LHC and the Critical p+Pb Missing Link

Miklos Gyulassy
FIAS Frankfurt / Columbia Univ

1. Elliptic Flow at RHIC and its “Perfect Fluid” sQGP core interpretation
2. The Color Glass Condensate Challenge to above
3. Challenge² to CGC sharp surface and the Geometry of AA
4. Broken CGC and the rediscovery of the LUND model ?
5. Needed pA Control of Initial sQGP Geometry and Eccentricity

(collab.: D.Molnar, T.Hirano, L.McLerran, A.Adil, ...)

Inseparable Links:

$$pp \leftrightarrow pA \leftrightarrow AA$$

Some references:

New forms of QCD matter discovered at RHIC.

[Miklos Gyulassy](#) , [Larry McLerran](#) Nucl.Phys.A750:30-63,2005. nucl-th/0405013

Perfect fluidity of the quark gluon plasma core as seen through its dissipative hadronic corona.

[Tetsufumi Hirano](#), [Miklos Gyulassy](#) Nucl.Phys.A769:71-94,2006. nucl-th/0506049

Relativistic Hydrodynamics at RHIC and LHC.

[Tetsufumi Hirano](#) e-Print: arXiv:0704.1699

Hadronic dissipative effects on elliptic flow in ultrarelativistic heavy-ion collisions.

[Tetsufumi Hirano](#) et al Phys.Lett.B636:299-304,2006. e-Print: nucl-th/0511046

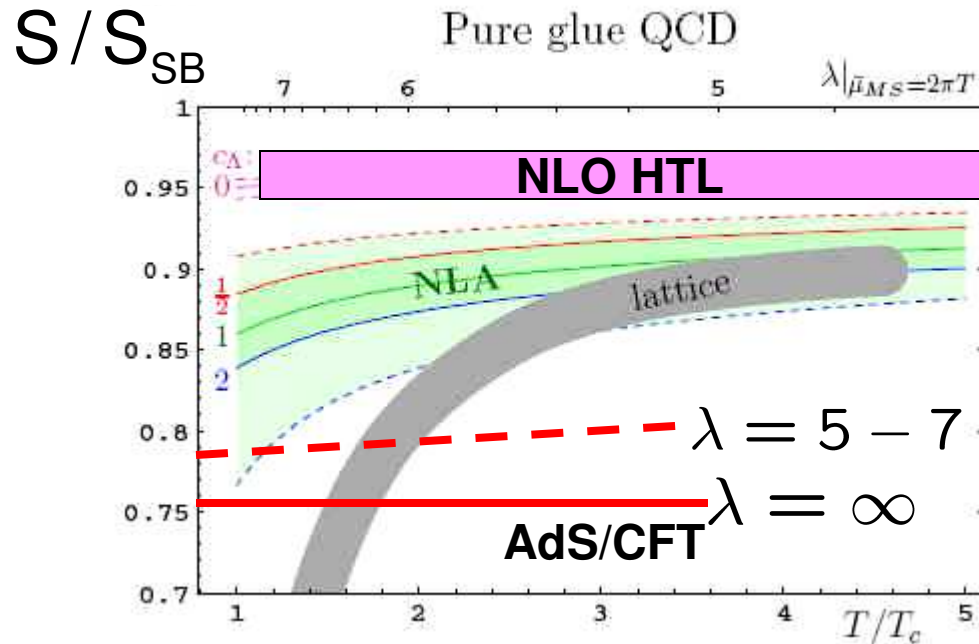
CGC vs Glauber geom refs.

Adil & Gyulassy, Phys. Rev. C 72 (2005) 034907

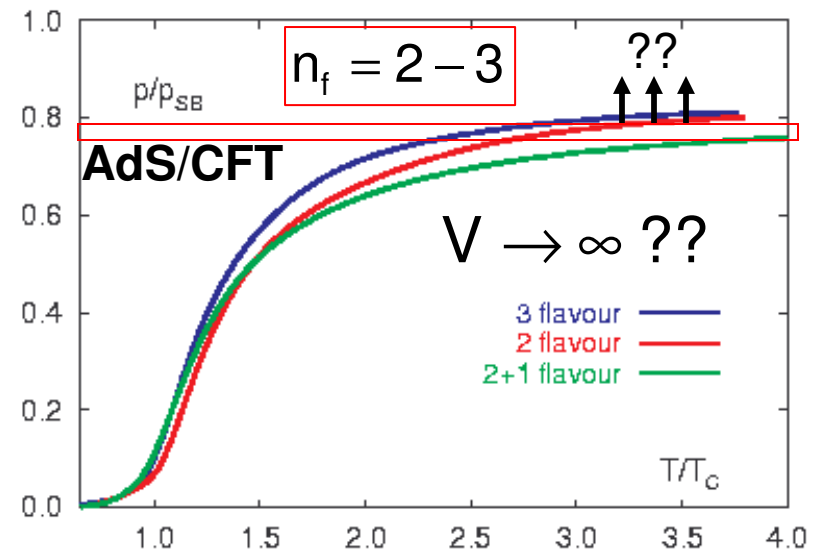
Adil, Gyulassy & Hirano , Phys. Rev. D 73 (2006) 074006

Adil, Drescher, Dumitru, Hayashigaki & Nara, PRC 74 (2006) 044905

What is a strongly coupled Quark Gluon Plasma (sQGP) ?



Lattice QCD: F. Karsch et al



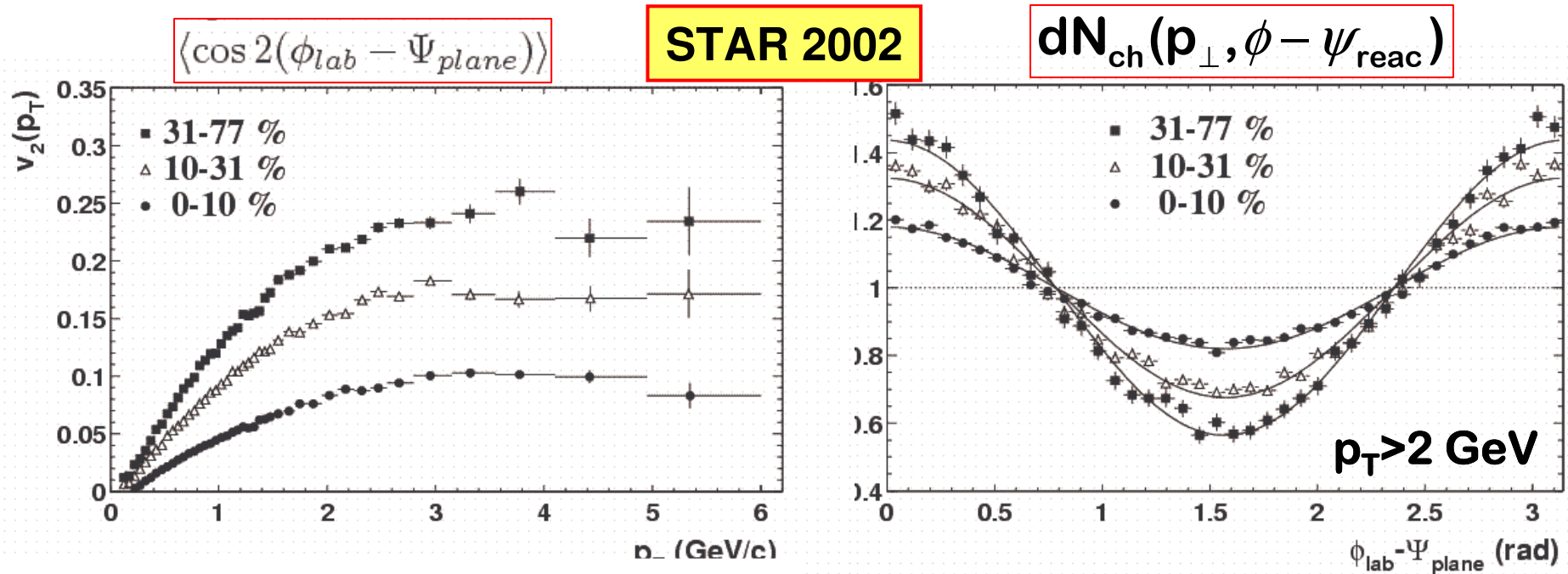
How to explain LQCD tiny 15% deviation from Stefan-Boltzmann for $T > 2T_c$?? Is the sQGP an AdS_5 Black Hole?
or simply a screened massive quasiparticle gas?

No approximation is accurate enough yet to tell

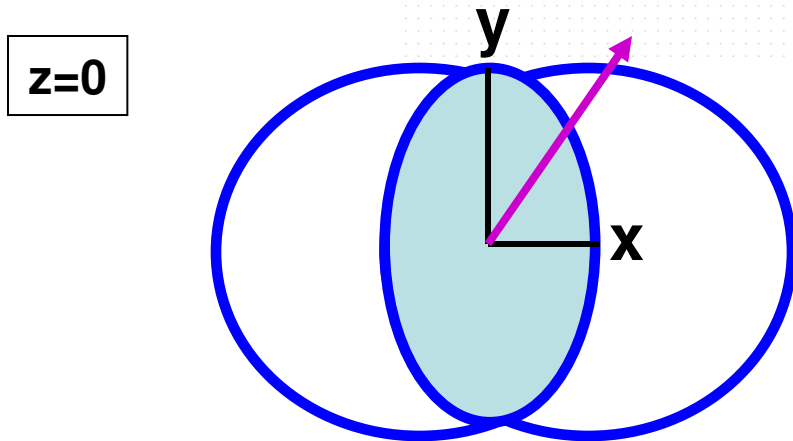
Hard-thermal-loop entropy of supersymmetric Yang-Mills theories.

[J.-P. Blaizot](#), [E. Iancu](#), [U. Kraemmer](#), [A. Rebhan](#) e-Print: [hep-ph/0611393](#)

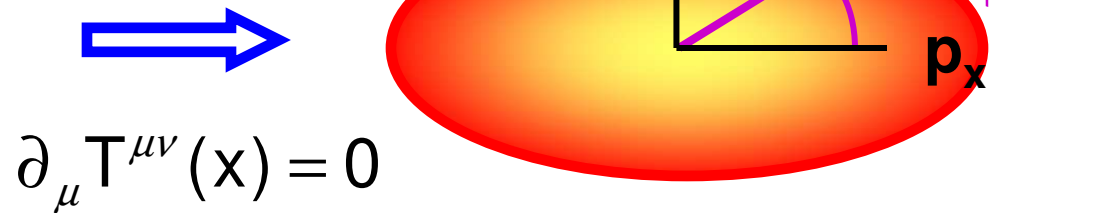
Discovery of Transverse Elliptic Flow in Non-central Au+Au at RHIC



Initial spatial anisotropy



Final momentum anisotropy



$$\partial_\mu T^{\mu\nu}(x) = 0$$

Early Universe was a liquid

Quark-gluon blob surprises particle physicists.

by Mark Peplow
news@nature.com

nature

The Universe consisted of a perfect liquid in its first moments, according to results from an atom-smashing experiment.

Scientists at the Relativistic Heavy Ion Collider (RHIC) at Brookhaven National Laboratory on Long Island, New York, have spent five years searching for the quark-gluon plasma that is thought to have filled our Universe in the first microseconds of its existence. Most of them are now convinced they have found it. But, strangely, it seems to be a liquid rather than the expected hot gas.

BNL

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Brookhaven

Universe May Have Begun as Liquid, Not Gas

Associated Press
Tuesday, April 19, 2005; Page A05

The Washington Post

New results from a particle collider suggest that the universe behaved like a liquid in its earliest moments, not the fiery gas that was thought to have pervaded the first microseconds of existence.

Early Universe was 'liquid-like'

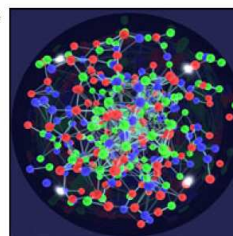
Physicists say they have created a new state of hot, dense matter by crashing together the nuclei of gold atoms.

BBC NEWS

The high-energy collisions prised open the nuclei to reveal their most basic particles, known as quarks and gluons.

The researchers, at the US Brookhaven National Laboratory, say these particles were seen to behave as an almost perfect "liquid".

The work is expected to help scientists explain the conditions that existed just milliseconds after the Big Bang.



The impression is of matter that is more strongly interacting than predicted

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Contact: Karen McNulty Walsh, (631) 344-8350 or Mona S. Rowe, (631) 344-5056

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RHIC Scientists Serve Up "Perfect" Liquid

New State of Matter Is 'Nearly Perfect' Liquid

New state of matter more remarkable than many new questions

April 18, 2005

TAMPA, FL -- The four detector groups at the Relativistic Heavy Ion Collider (RHIC), the U.S. Department of Energy's Brookhaven National Laboratory, announced today that they have created what appears to be a new state of matter out of the building blocks of atomic nuclei, quarks and gluons. The researchers unveiled their findings--which could provide new insight into the composition of the universe just moments after the big bang--today in Florida at a meeting of the American Physical Society.

Physicists working at Brookhaven National Laboratory announced today that they have created what appears to be a new state of matter out of the building blocks of atomic nuclei, quarks and gluons. The researchers unveiled their findings--which could provide new insight into the composition of the universe just moments after the big bang--today in Florida at a meeting of the American Physical Society.

SCIENTIFIC AMERICAN

There are four collaborations, dubbed BRAHMS, PHENIX, PHOBOS and STAR, working at Brookhaven's Relativistic Heavy Ion Collider (RHIC). All of them study what happens when two interacting beams of gold ions smash into one another at great velocities, resulting in thousands of subatomic collisions every second. When the researchers analyzed the patterns of the atoms' trajectories after these collisions, they found that the particles produced in the collisions tended to move collectively, much like a school of fish does. Brookhaven's associate laboratory director for high energy and nuclear physics, Sam Aronson, remarks that "the degree of collective interaction, rapid thermalization and extremely low viscosity of the matter being formed at RHIC make this the most nearly perfect liquid ever observed."



Image: BNL

of hot, dense matter by crashing together the nuclei of gold atoms. The researchers unveiled their findings--which could provide new insight into the composition of the universe just moments after the big bang--today in Florida at a meeting of the American Physical Society.

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the matter created in RHIC's heavy ion collisions

The coming year will see a number of interesting developments as the Large Hadron Collider (LHC) goes online. The enormous amount of data generated by the LHC will force us to refine our methods—and explore new ones—for extracting and interpreting information from high energy collisions. This work should lead to new insights into the masses of elementary particles and the consequences of various models for particle physics and cosmology.

Also of interest is the recent application of string theory to the physics being done at the Relativistic Heavy Ion Collider (RHIC), where string theory permits some calculations that would otherwise be intractable. The idea at RHIC is to better understand the strong force that binds together the elements of a nucleon, and 2007 may see the theoretical advances of string theory inform the experimental results from RHIC.

—Lisa Randall, Harvard University

**Of course, some may disagree...
...but in the end the “right” approach
will be validated by both
qualitative concepts,
and quantitative predictions**



New Yorker, Jan. 8, 2007

(from P. Steinberg, LRP07)

How does QCD/Nuclear matter **Flow** ??

$$\eta_{\text{H}_2\text{O}} = 1 \text{ cP} = 2 \times 10^{-15} \frac{\text{GeV}}{\text{fm}^2 \cdot \text{c}}$$

$$\eta_{\text{Lava}} = 10^5 \text{ cP}$$



Pahoehoe

$$\eta_{\text{Hadron}} = \frac{T}{\sigma_H c} = \frac{1}{10} \left(\frac{\text{GeV}}{\text{fm}^2 \cdot \text{c}} \right) \left(\frac{T}{T_c} \right) = (5 \times 10^{13} \text{ cP}) \left(\frac{T}{T_c} \right)$$

$$\eta_{\text{Hadron}} \sim 100 \eta_{\text{Granite}}$$

Fluid Evolution in 1+1 D Bjorken Expansion

$$\begin{aligned}
 \text{Entropy Density} & \quad \text{Shear (+ } \frac{3}{4} \text{ Bulk) Viscosity} \\
 \uparrow & \quad \quad \quad \uparrow \quad \quad \quad \leftarrow \\
 \frac{d\epsilon}{d\tau} &= -sT/\tau & \text{Perfect Euler Fluid} \\
 &= -(sT/\tau)[1 - 4(\eta/s)/3T\tau] & \text{ImPerfect Fluid} \\
 \uparrow & & \\
 \text{Energy} & & \\
 \text{Density} & & \\
 & \quad \quad \quad \text{(first order Navier-Stokes)}
 \end{aligned}$$

At early times $\tau \sim 1/T$ the dimensionless ratio η/s
 Measures the importance of dissipative effects
 That reduced the transfer of heat into collective flow

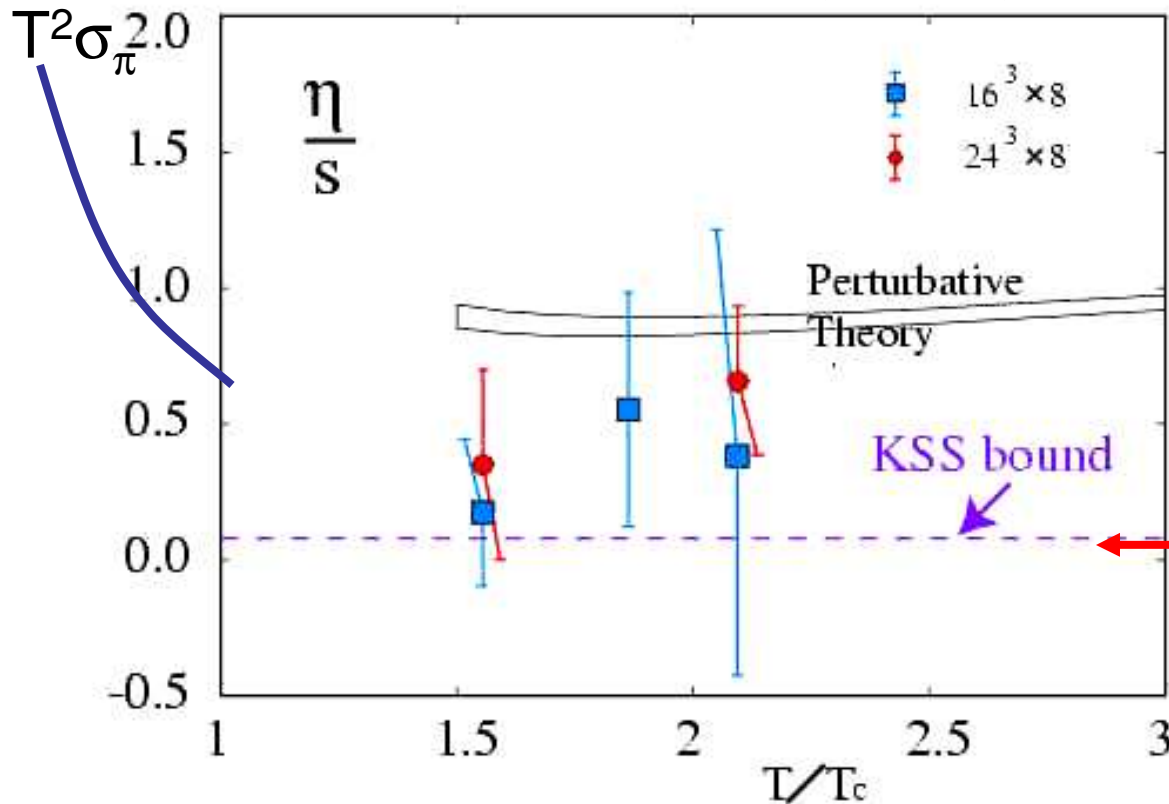
At late times $\tau \gg (\eta/s) 1/T$ longitudinal gradients are small
 But 1D \rightarrow 3 D and T drops rapidly below T_c

Transport coefficients of a gluon plasma

Lattice QCD vs pQCD vs AdS/CFT N=4 SYM

Gavin 85
1

Lattice QCD: A.Nakamura,S.Sakai, 2004



Danielewicz, MG, (1985) *

Perturbative QCD

$$\frac{T \lambda_{\text{pQCD}}}{5} \approx \frac{(0.3)^2}{\alpha^2 \log 1/\alpha} \sim 1$$

$$\left(\frac{\eta}{\sigma} \right)_{\text{adS/CFT}} = \frac{1}{4\pi}$$

N=4 SUSY
 $g^2 N_c \rightarrow \infty$

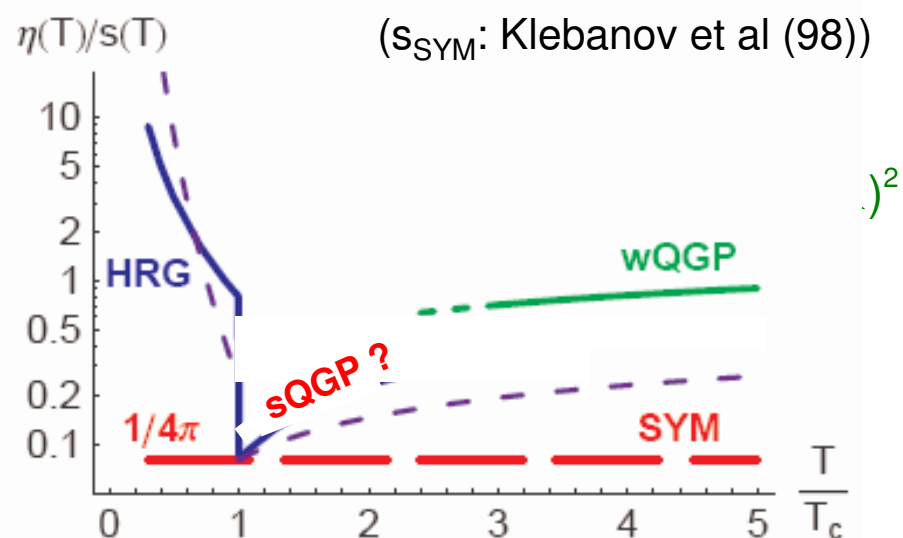
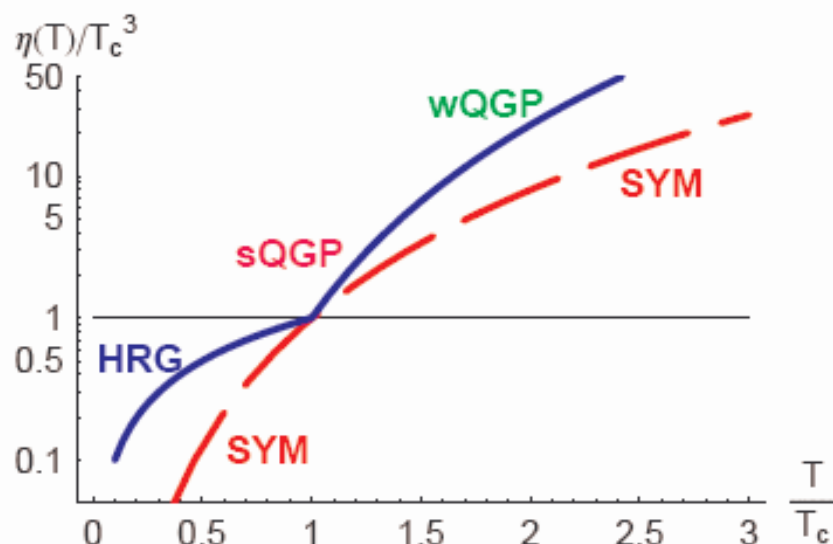
$$\frac{T \lambda_{\text{min}}}{5} \approx \frac{\hbar = 1}{15}$$

N=4 SUSY KSS: Kovtun,Son,Starinets 04

The Perfect Fluidity of QGP Core may be a Signature of Deconfinement

T. Hirano and MG Nucl.Phys.A769:71-94,2006

$\eta(T)$: shear viscosity and $s(T)$: entropy density



- Absolute value of viscosity

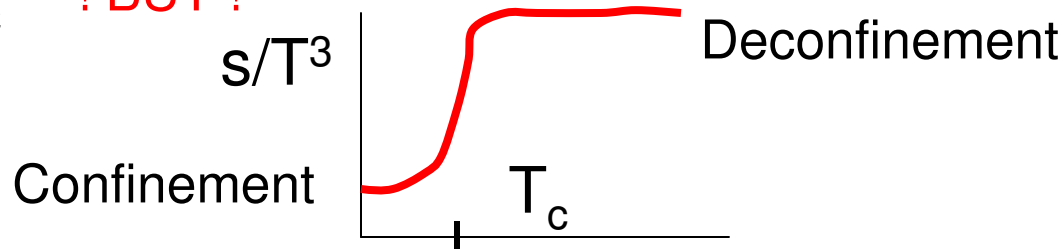
$$\eta(\text{sQGP}) > \eta(\text{hadron})$$

Viscosity is monotonic
Increasing with T

! BUT !

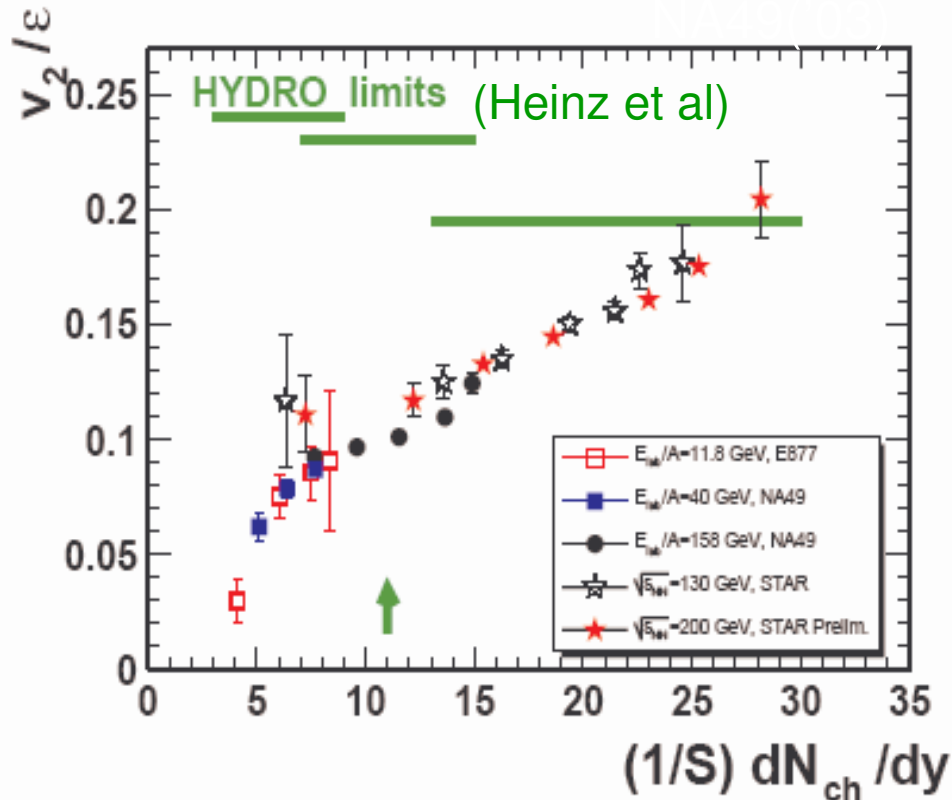
- Ratio to entropy density

$$\eta/s(\text{sQGP}) \ll \eta/s(\text{hadron})$$

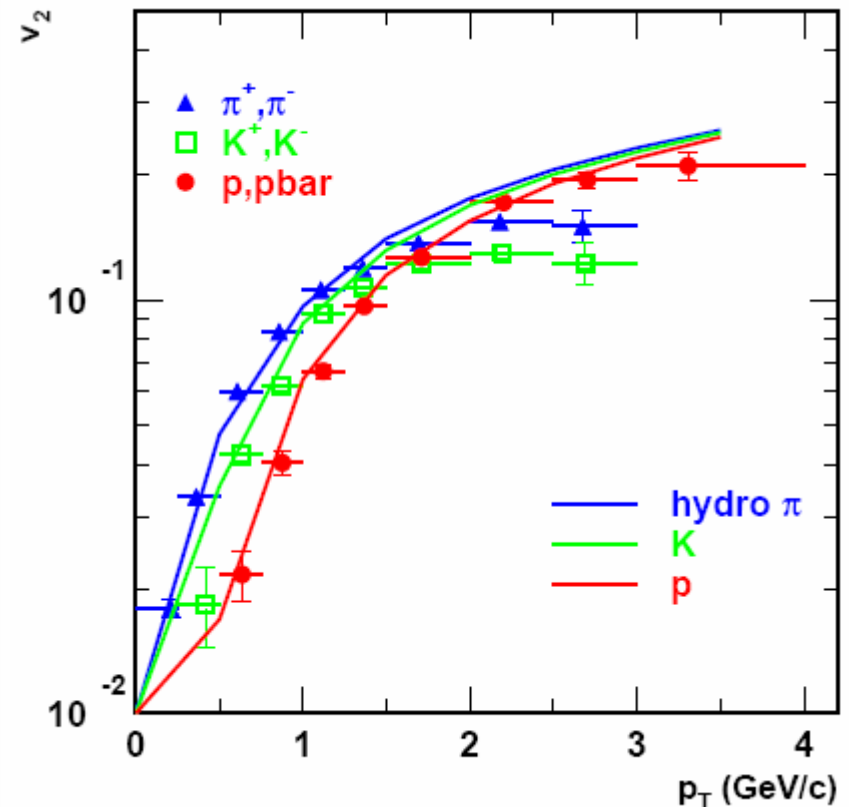


Basis of the BNL Press Release

Integrated elliptic flow



Differential elliptic flow



Perfect Fluid (zero viscosity) Hydrodynamics appears to do “work” for the first time in central AuAu at highest RHIC energy

At lower energies Perfect Fluidity is Obscured by the highly dissipative Hadron Resonance Corona

Bass, Dumitru,...
Teaney, Shuryak
Hirano, Nara

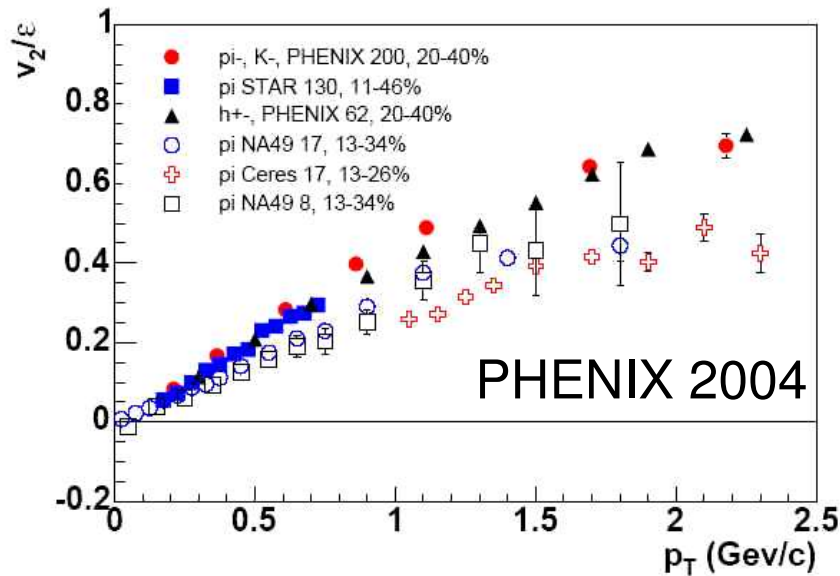
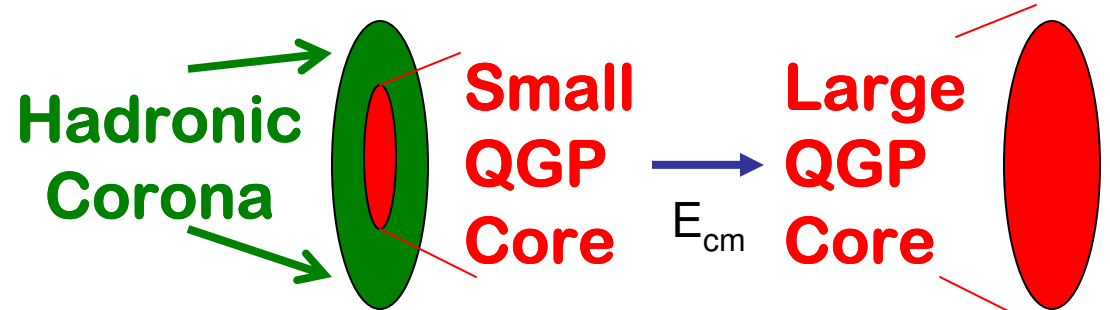


FIG. 16: $v_2(p_T)/\epsilon$ versus p_T for mid-central collisions at RHIC (filled symbols) and SPS (open symbols). Dividing by eccentricity removes to first order the effect of different centrality selections across the experiments.

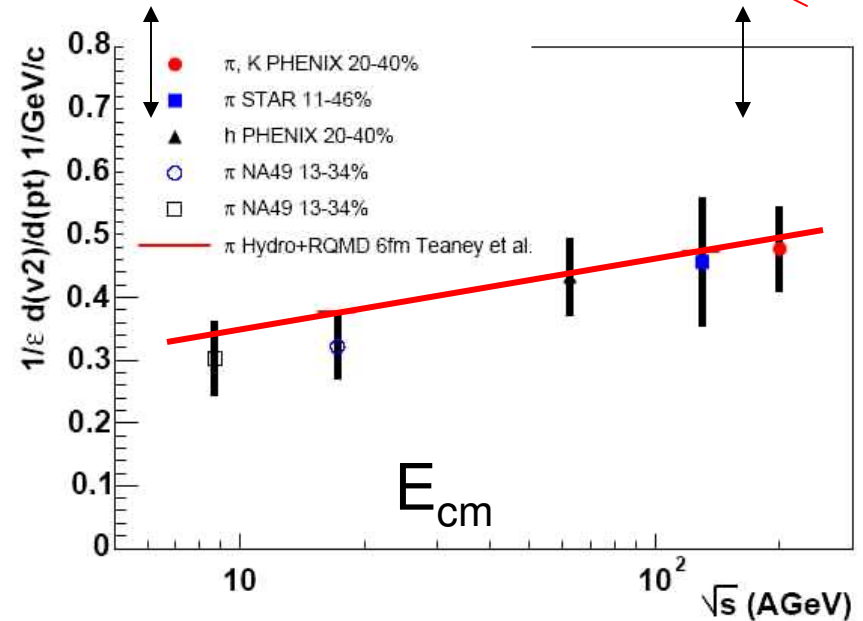
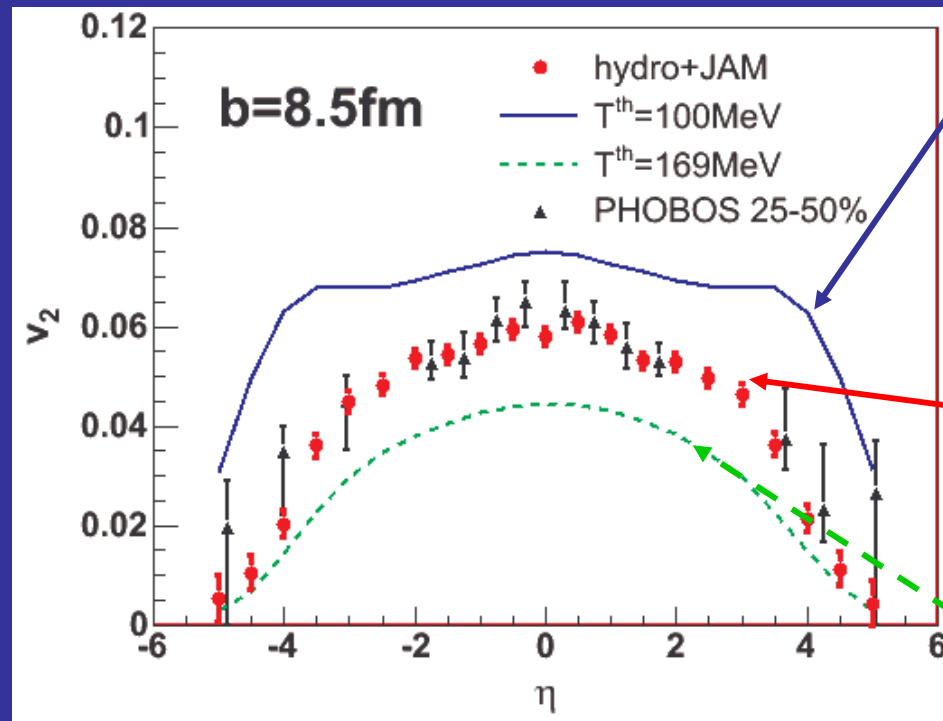


FIG. 17: The slope of the scaled elliptic flow, $(dv_2/dp_T)/\epsilon$, for mid-central collisions at RHIC (filled symbols) and the SPS (open symbols). The slope is calculated for the data $p_T < 1$ GeV/c. The solid error bars are the systematic errors that include the systematic error on v_2 and ϵ .

Elliptic Flow --Rapidity Dependence--



QGP+hadron perfect fluids

- overshoots data

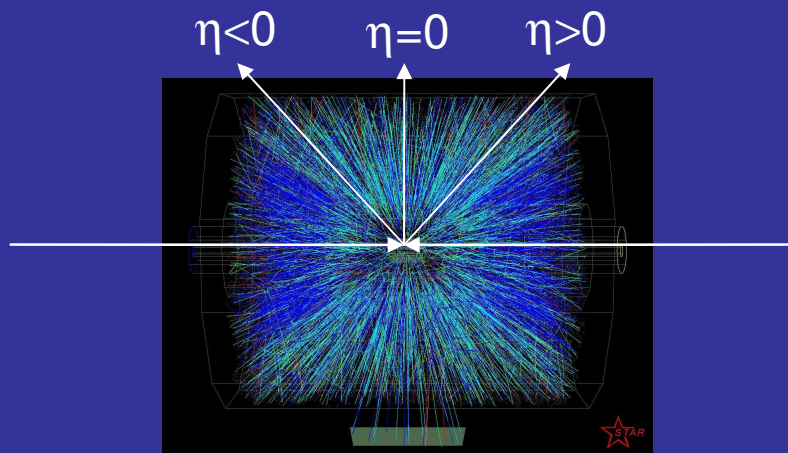
Away from mid rapid

QGP perfect fluid core
+ hadron gas corona

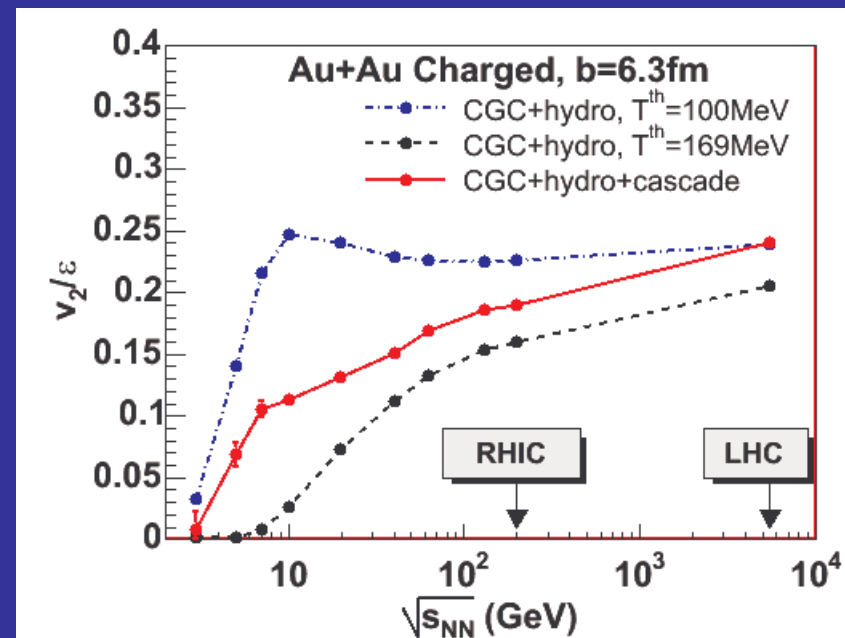
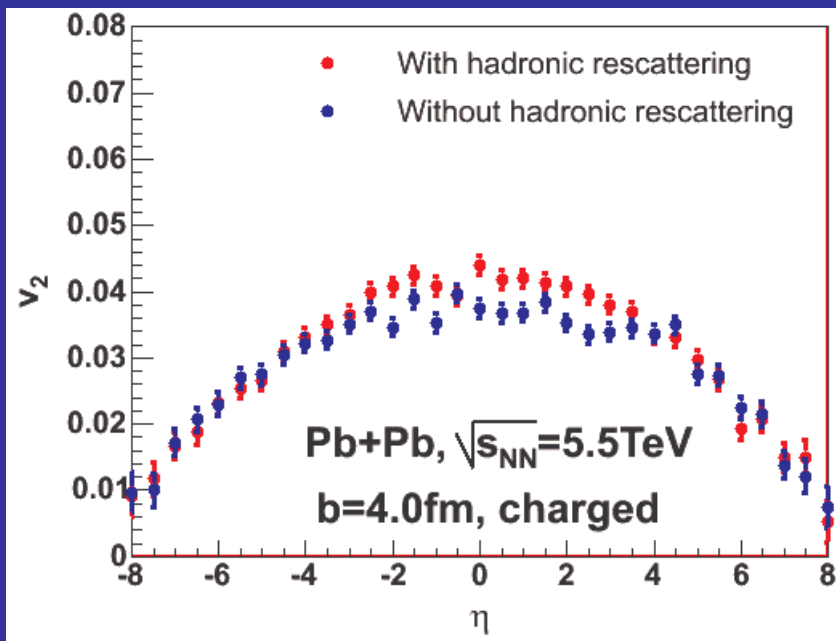
- Agrees with data

QGP fluid only ($T_F=T_c$)
no hadronic rescatterings

- undershoots data in whole region



$v_2(\eta)$ @ and $v_2(\sqrt{s_{NN}})$



- Total v_2 generated mainly in the sQGP core

- v_2/ϵ increases somewhat in this hybrid Q Fluid + H Gas model

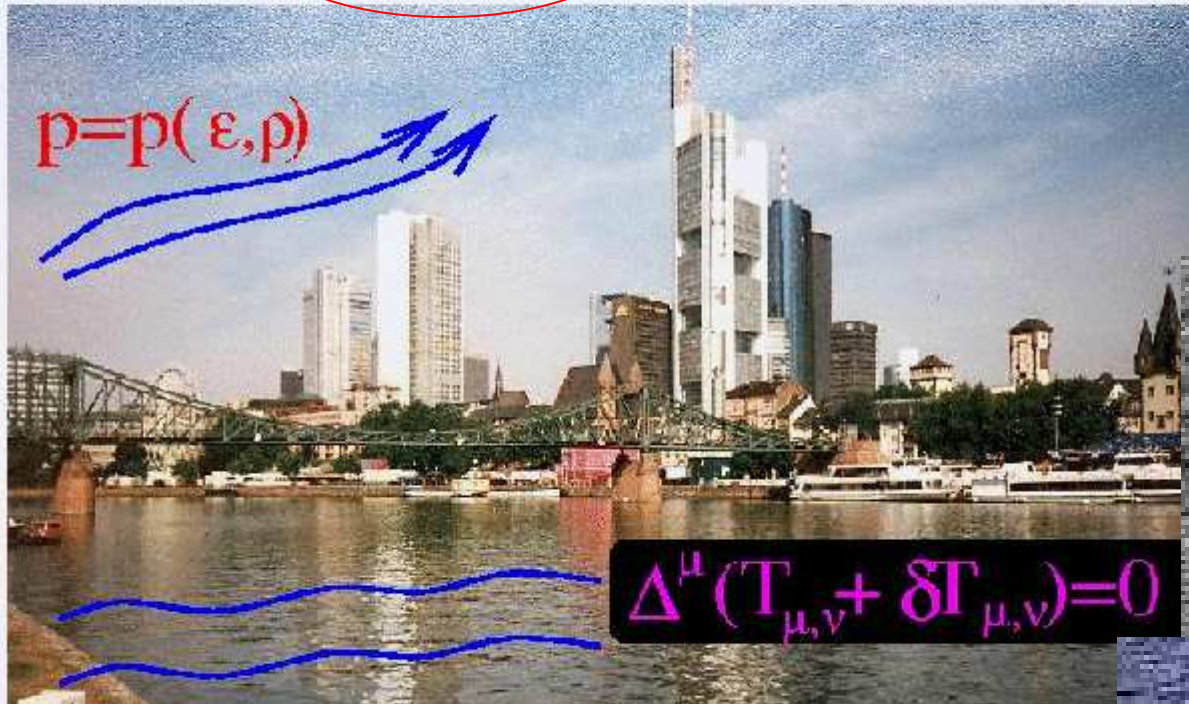
v_2^{LHC} can increase substantially only IF Initial geometry does!

Teaney et al.('02)

Wrestling with Monsters and Uncertainties in the Perfect Fluid

NCRH2007

Numerical and Conceptual Issues in Relativistic Hydrodynamics



Frankfurt Institute for Advanced Studies, 16-19 April 2007

<http://th.physik.uni-frankfurt.de/~ncrh/>
Giorgio Torrieri (ITP)

Complex competing Interplay of 3+1D Hydro in A+A

- 1) Elliptic Flow
- 2) Radial Flow
- 3) Longitudinal Flow

Chemical FreezeOut leads to more rapid cooling
That amplifies azimuthal flow asymmetry.
This requires Hadronic dissipation to reduce asymmetry

In Chem Equilib less rapid cooling keeps v_2 near data
and there is no room for dissipation but at
the unacceptable cost of losing the Hadron Chemistry

A Cold Splash on the Perfect Fluid?



Part II: The CGC_{KLN} Challenge to sQGP

CGC Initial Conditions

- + Perfect sQGP Fluid core
- + Hadron Gas corona

= Overprediction of v_2 !

Hirano, Nara, Heinz, Kharzeev, ...
Dumitru, Nara, Drescher

Gluon Saturation Models

- EKRT: Final State Saturation

$$\frac{3}{2} \frac{dN_{\text{ch}}}{dy} \stackrel{\Delta S=0}{=} \frac{dN_{AA \rightarrow g}^{\text{pQCD}}}{dy} = Q_{\text{sat}}^2 R^2 \approx 1.16 A^{0.92} (\sqrt{s})^{0.40}$$

$$Q_{\text{sat}}(A, s) \approx 0.208 A^{0.128} (\sqrt{s})^{0.191}$$

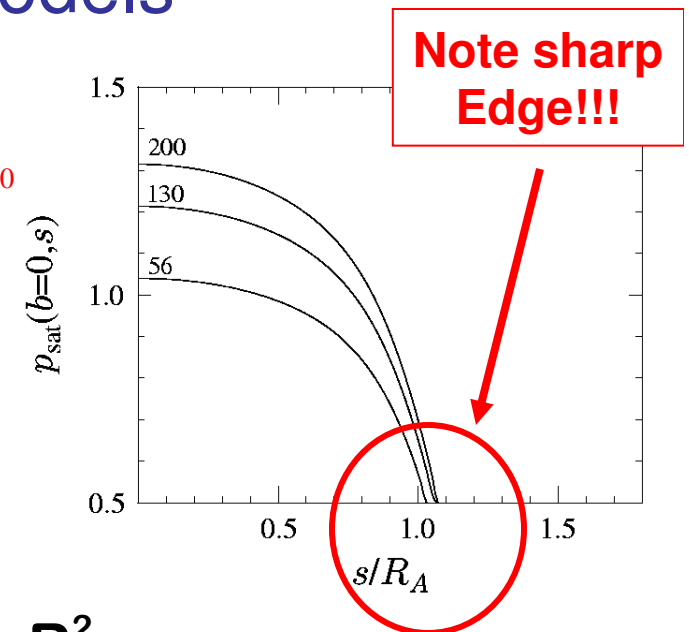
- Mueller, Qiu, Blaizot : Initial State Saturation

$$\frac{dN_{\text{glue}}^{\text{max}}}{dy} = 2 \times G_A(x, Q_{\text{sat}}^2) \Big|_{x=2Q/\sqrt{s}} = \left(\frac{c_s}{g^2} \right) Q_{\text{sat}}^2 R^2$$

- McLerran, Venugopalan, Krasnitz: Color Glass Condensate
Classical Yang-Mills on a Lattice

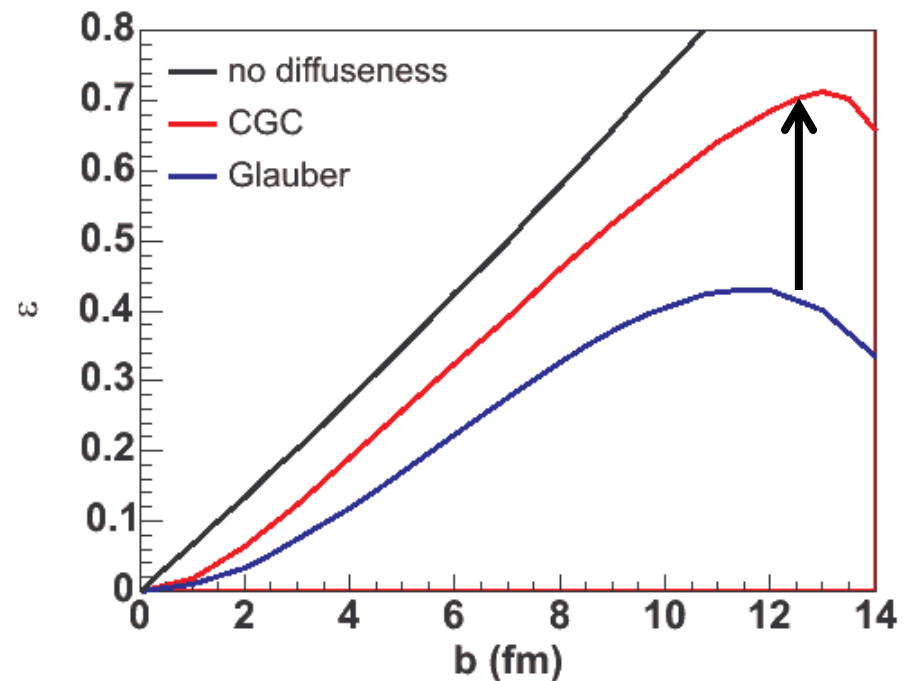
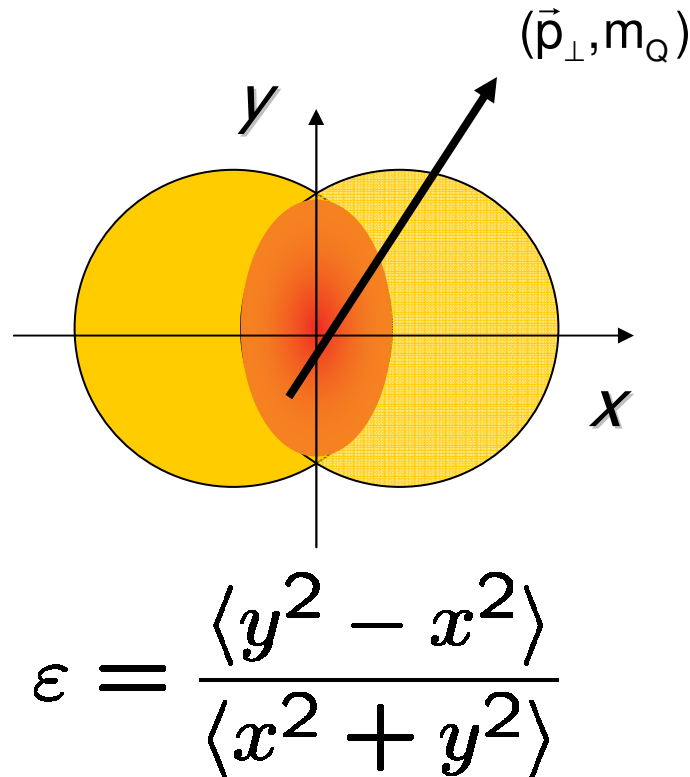
- Kharzeev, Levin, Nardi : Analytic CGC Model

$$\frac{dN_g^{\text{CGC}}}{dy} = 2 \times G_A\left(x = \frac{2Q_{\text{sat}}}{\sqrt{s}}, Q_{\text{sat}}^2\right) = c \frac{Q_{\text{sat}}^2 R^2}{\alpha_s(Q_{\text{sat}}^2)}$$



Initial Transverse Geometry: CGC vs Glauber

Sharper edge
Increases ε



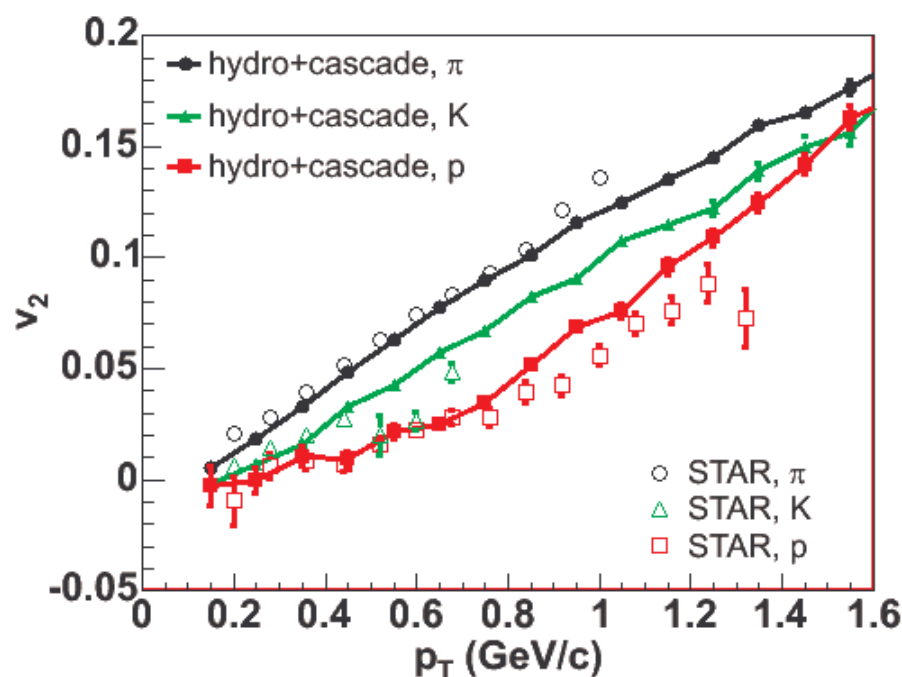
Data => Perfect Fluid core only if
Data => **Im**perfect (viscous) if

$$v_2^{\text{exp}} \approx 0.2 \varepsilon_{\text{geom}}$$

$$v_2^{\text{exp}} < 0.2 \varepsilon_{\text{geom}}$$

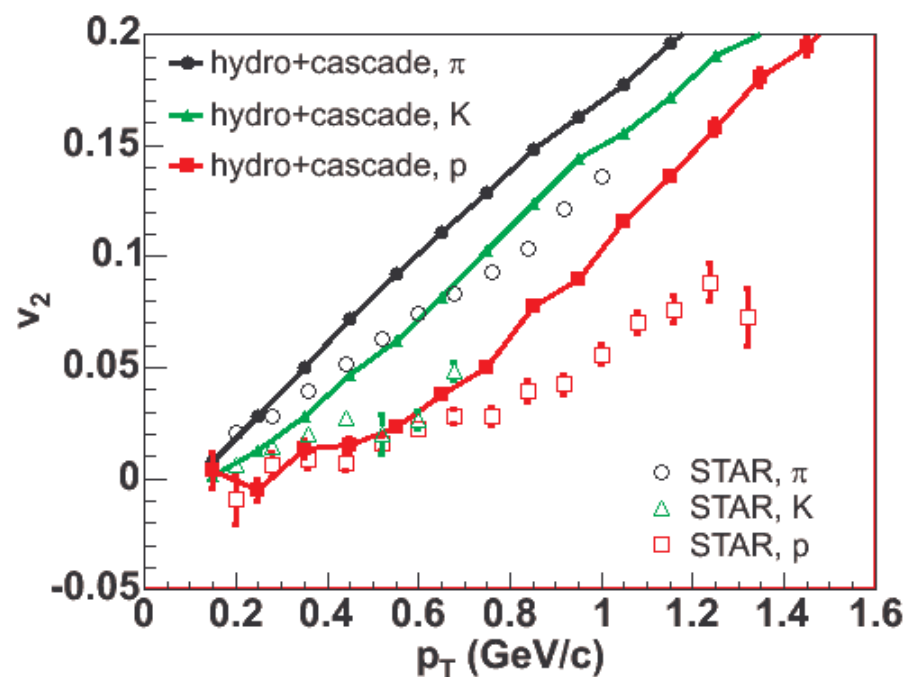
Differential Elliptic Flow $v_2(p_T, m)$ for identified hadrons π, K, p

Glauber Initial Condition



$v_2(\text{Glauber}) \sim v_2(\text{data})$

CGC Initial Condition



$v_2(\text{CGC}) > v_2(\text{data}) !!$

Glauber Geom + v_2 Data \Rightarrow “sQGP” is Perfect Fluid

CGC Geom + v_2 Data \Rightarrow “sQGP” is Imperfect Fluid !!

Perfect or Imperfect Fluidity

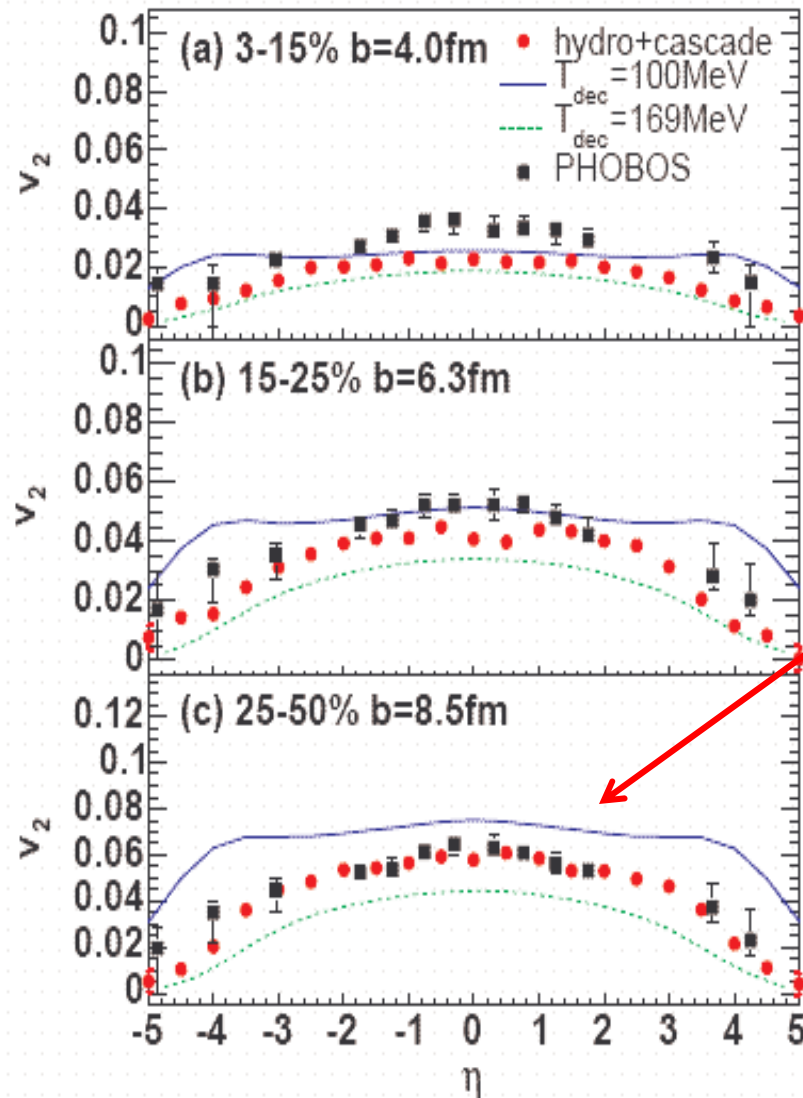


Depends on Initial Conditions



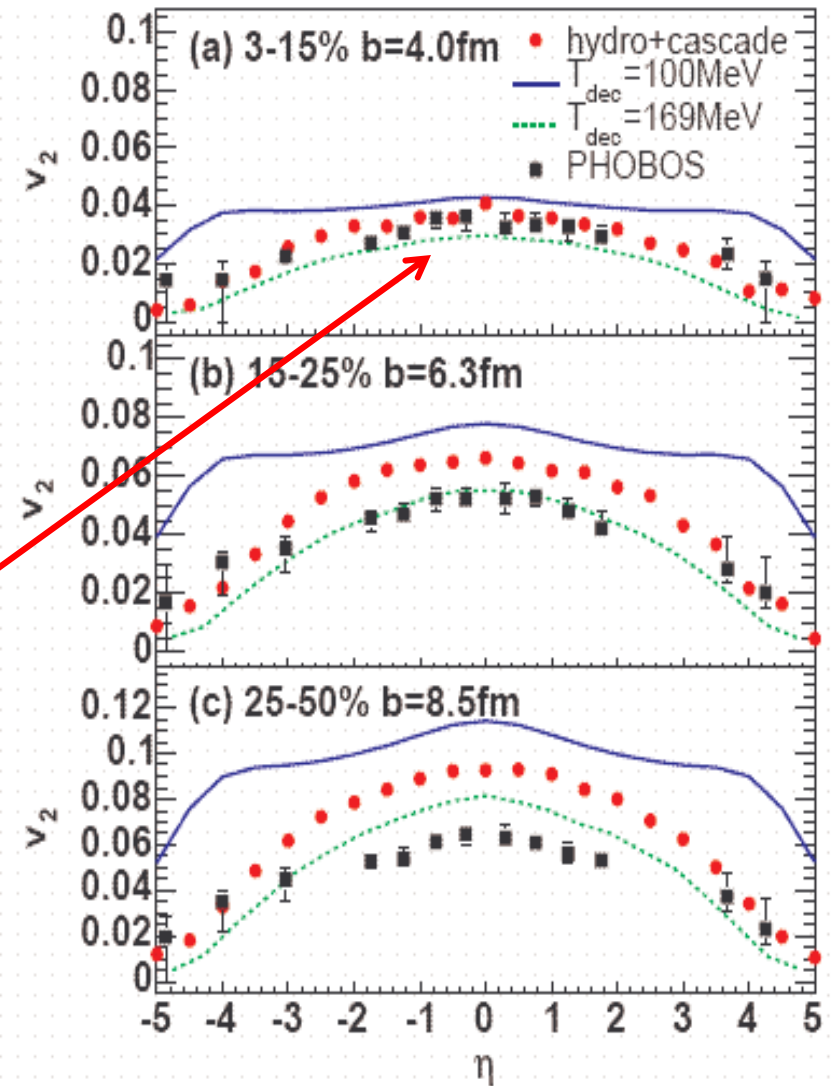
Hirano, Nara, et al 06

Glauber Participant Geometry



Glauber best in Peripheral

Color Glass Initial Conditions



CGC best in Central

My conclusion so far:

Perfect Fluid sQGP core can only “work”
If Initial AA geometry evolves from

Diffuse Glauber at large impact parameters

To

Sharp CGC geometry at small impact params

Equivalently: Glauber is right when $Q_{\text{sat}} < 1 \text{ GeV}$
CGC May be right when $Q_{\text{sat}} > 1 \text{ GeV}$

Dilute Surface region is always Glauber

Part III

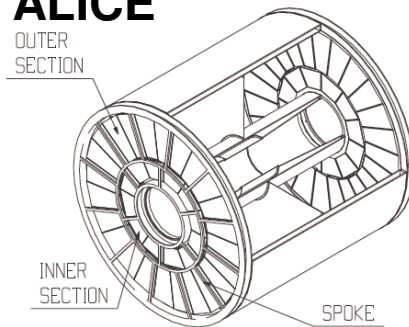
- Closer look at theory of AA
Initial Conditions

Hydro is simply a map from a given IC
To a specified FO=freeze-out hypersurface

$$IC(x,p) \rightarrow T^{\mu\nu}(t_0, \vec{x}) ; \quad \partial T = 0 \quad ; \quad T(\Sigma_{f.o.}), u^\mu(\Sigma_{f.o.}) \rightarrow dN/dydp_T$$

We have to control both IC and FO to extract viscosity/s

1995 ALICE



ALICE: Physics Performance Report, Volume II

2007 ALICE Today

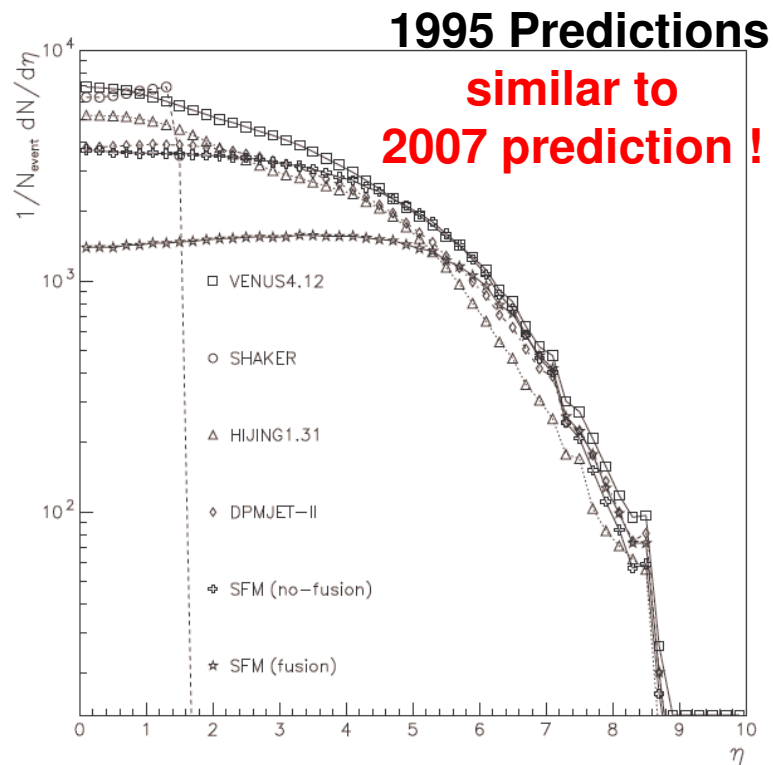
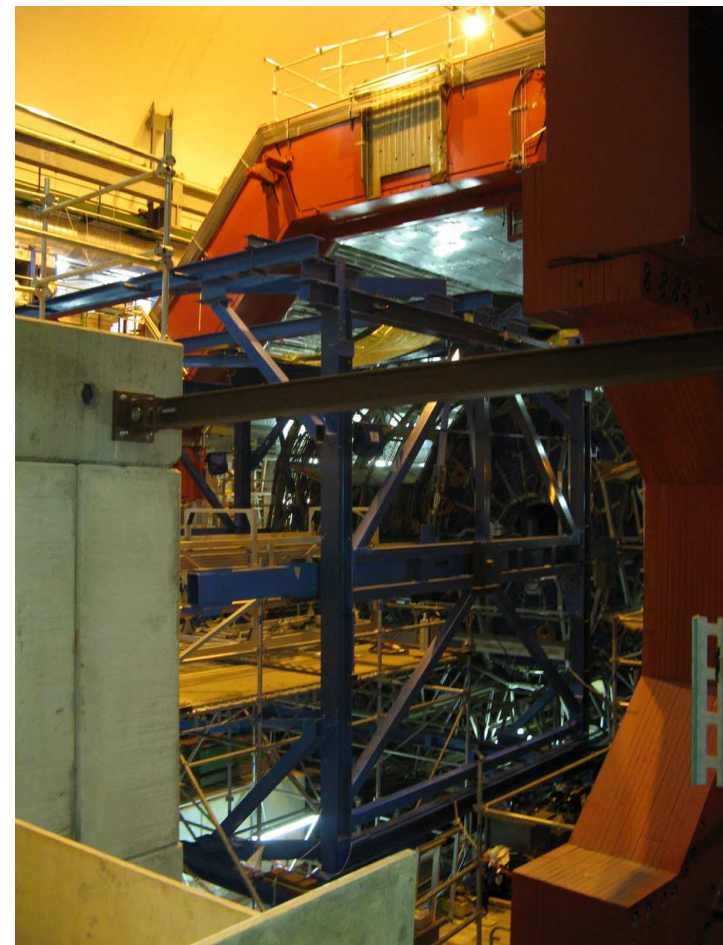
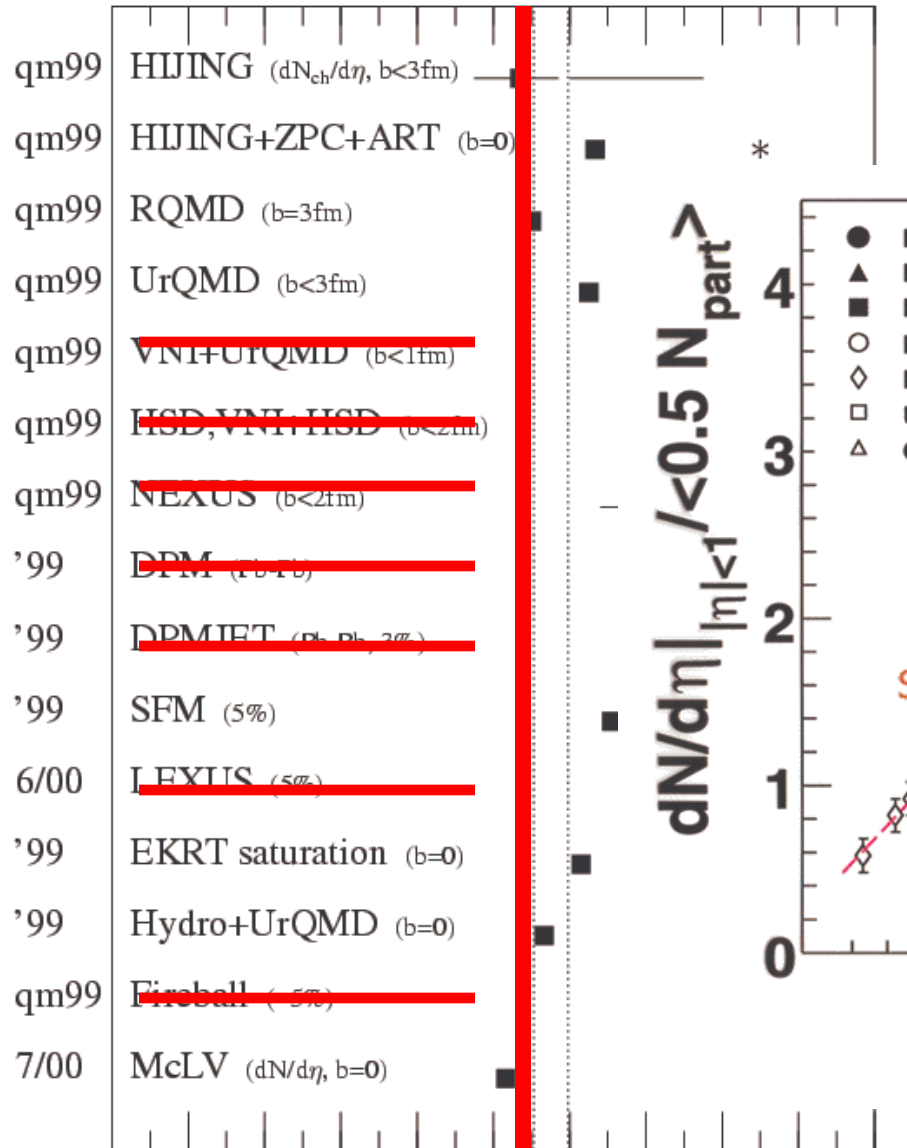


Figure 11.1: Charged particle multiplicities for central Pb–Pb events at a beam energy of 3 TeV per nucleon. The generators have been ordered by decreasing multiplicity at $\eta = 0$.

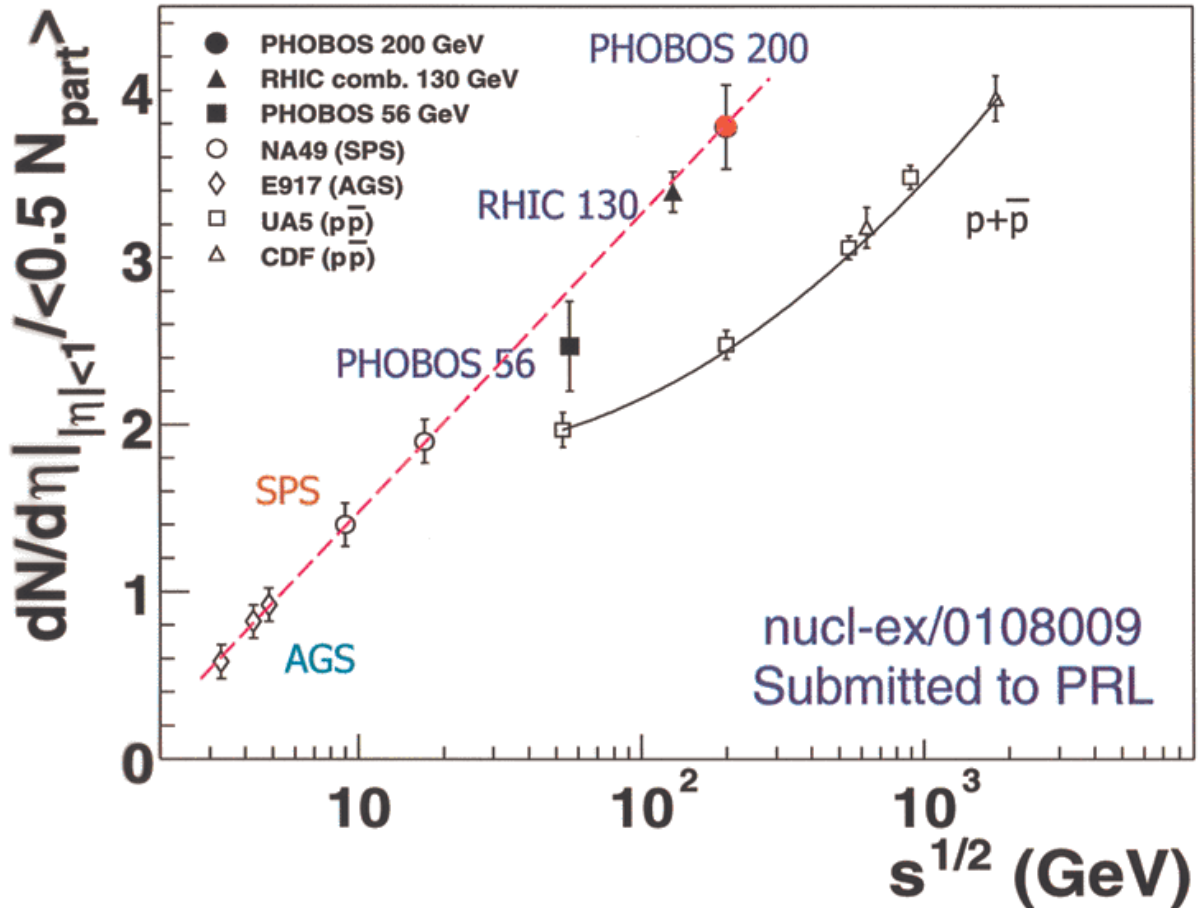


QM99 "Last Call for RHIC Predictions"

dN_{ch}/dy , Au+Au, $y=0$, $s^{1/2}=200$ AGeV
600 800 1000 1200 1400 1600



RHIC data



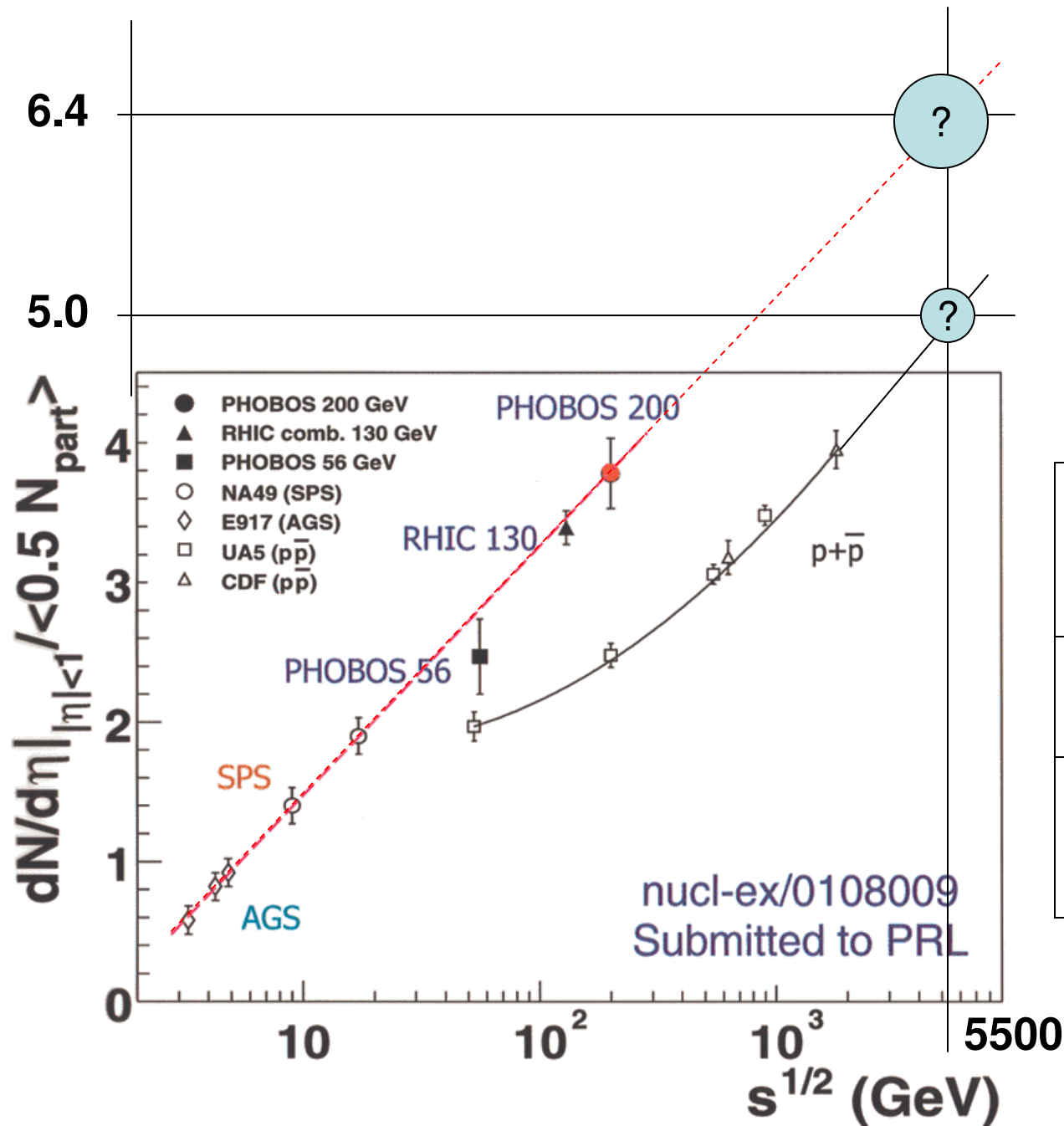
$\sim \frac{2}{3}$: $N(*) \rightarrow N_{ch}$ data * $(200/130)^{0.37} * 1.1$

~ 1.1 : $\eta \rightarrow y$

~ 0.9 : $b = 0 \rightarrow b \lesssim 3\text{fm}(5\%)$

Eskola QM01

Most Conservative PHOBOS LHC Extrapolation



Pb + Pb

$$\frac{dN_g^{LHC}}{dy} \sim 1700$$

$$s_{LHC} \sim 1.7 s_{RHIC}$$

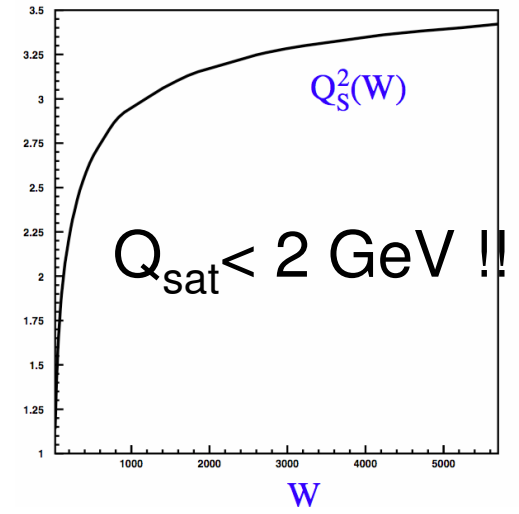
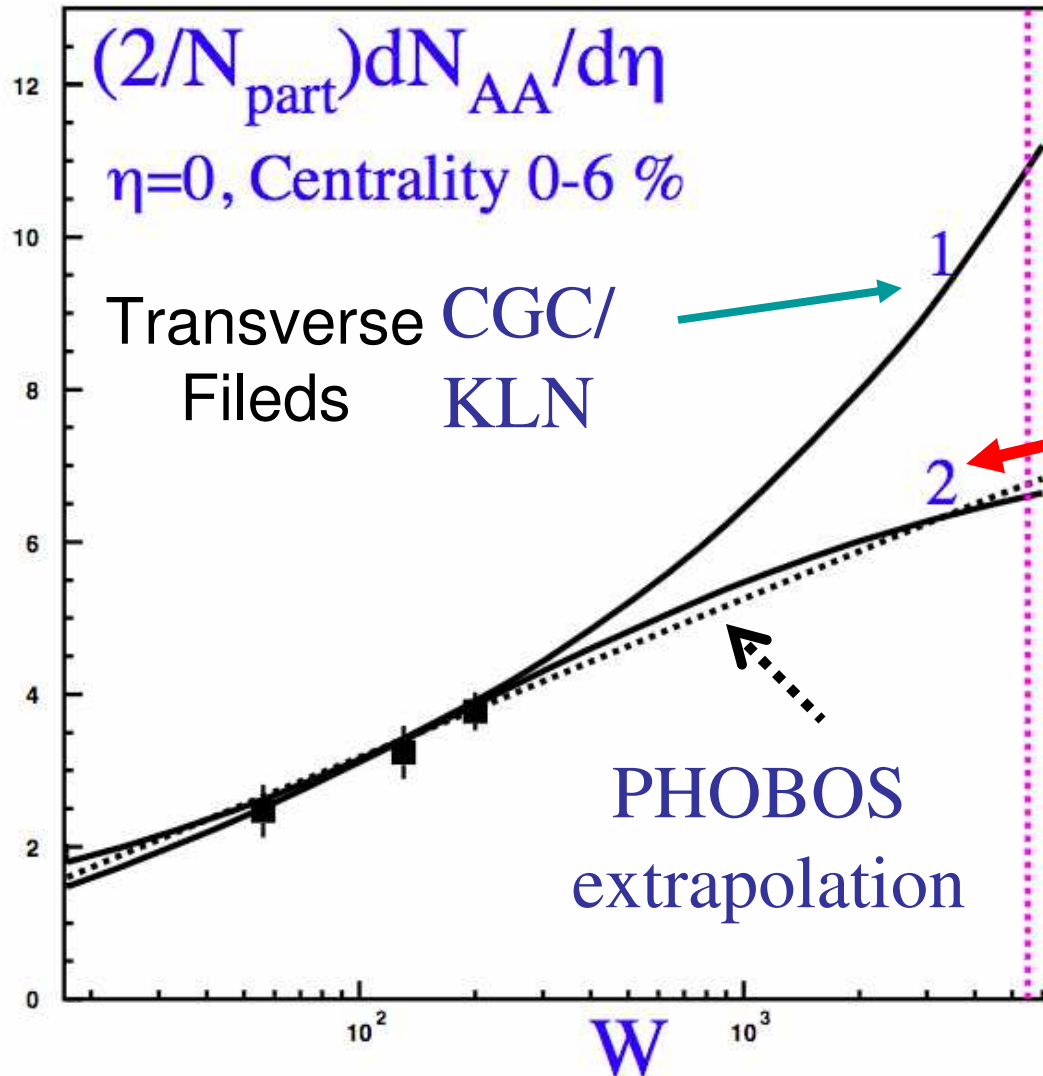
$$T_{LHC} \sim 1.2 T_{RHIC}$$

\sqrt{s}	$\frac{dN^{PbPb}}{208 \times dN^{pp}}$
200	1.52
5500	1.28

decrease ?

Kharzeev, Levin: Saturated Saturation The Broken Color Glass?

(or the rediscovery of the LUND model)



New
Longitudinal field
dominated
CGC

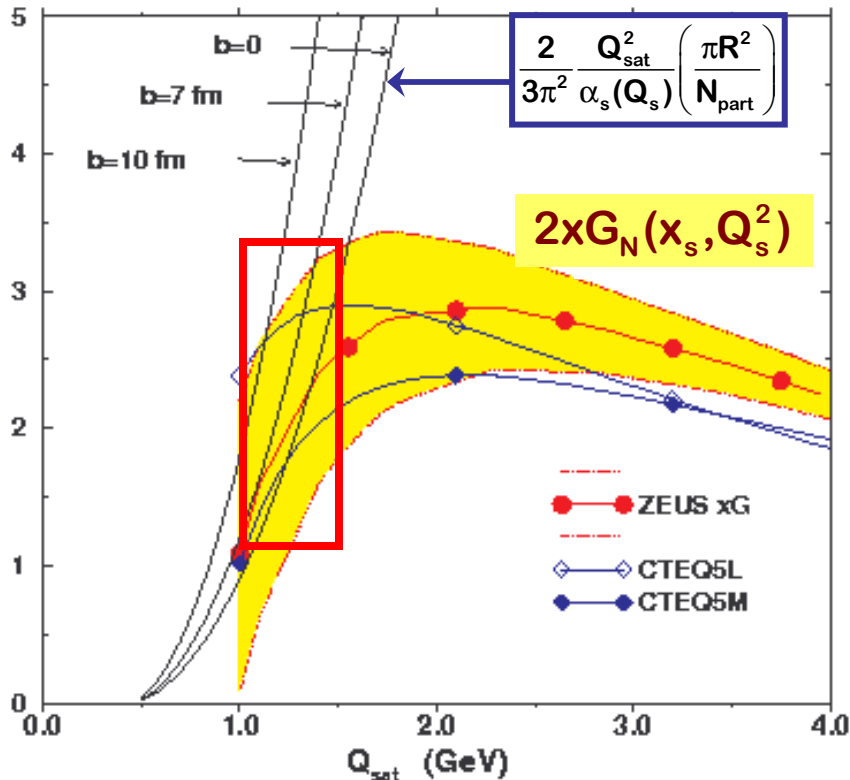
Kharzeev seminar
CERN 5/14/07

Initial State Saturation RHIC vs LHC

MGyulassy 02
unpublished

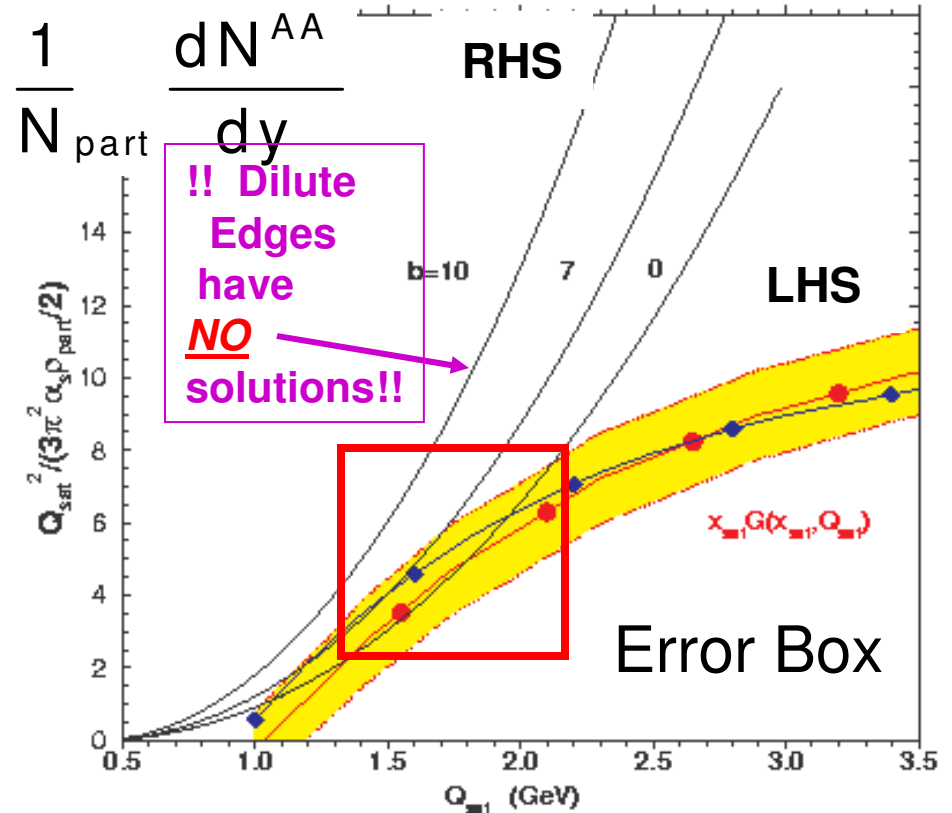
RHIC

Initial State Saturation at $E_{cm} = 130$ AGeV
Au + Au



LHC

Initial State Saturation at $E_{cm} = 5400$ AGeV



$$2xG_A(x = \frac{2Q_{sat}}{\sqrt{s}}, Q_{sat}^2) = \frac{2c}{3\pi^2} \frac{Q_{sat}^2 R^2}{\alpha_s(Q_s)}$$

$$2xG_p(x = \frac{2Q_{sat}}{\sqrt{s}}, Q_{sat}^2) = \frac{2c}{3\pi^2} \frac{Q_{sat}^2}{\alpha_s(Q_s)} \left(\frac{\pi R^2}{N_{part}} \right)$$

$$Q_s \propto A^{1/6} s^{\lambda/4}, \quad \lambda \approx 0.3$$

$$\frac{dN^{LHC}}{dy} \approx 800 - 3200$$

OK, our problem is that theoretically
The initial conditions at both RHIC and LHC
Are only understood to a factor ~ 2

And saturation models have large systematic uncertainties
In dilute regions of high b and/or interaction corona

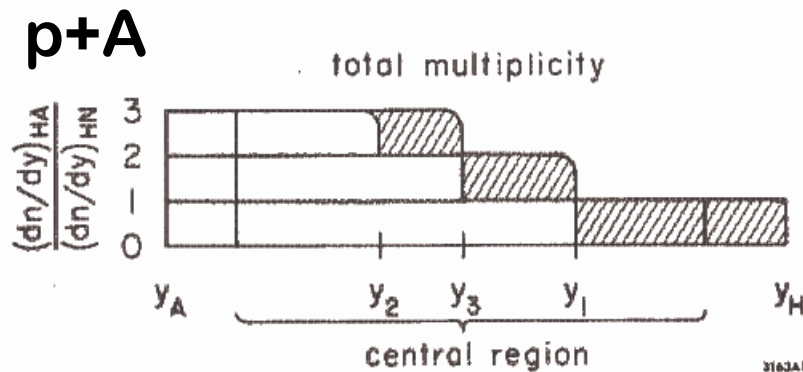
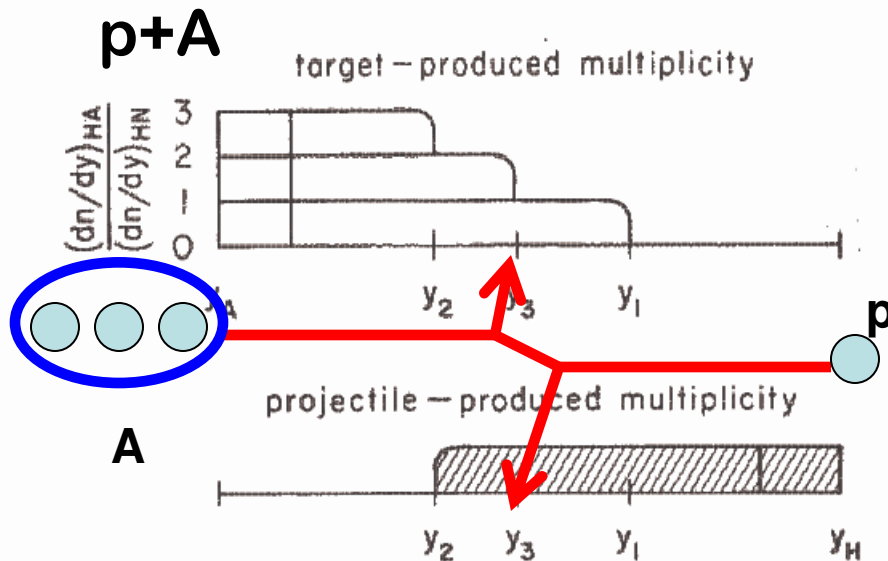
This is not good enough to resolve the perfection fluidity
Via $v_2(p_T, s, b)$ observables

We need independent experimental input
To help guide the theory

p+A at LHC please!

Brodsky, Gunion, Kuhn, PRL39(77)1120

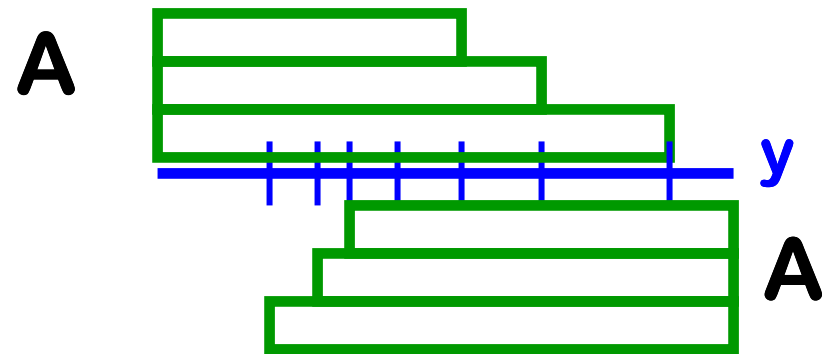
Multi-string Extensions of pp to p+A to A+A



$$A^{1/3} \geq \frac{dN_{pA}}{dN_{pp}} \geq 1 \quad \text{“pA Triangle”}$$

DPM: Capella et al

LUND: Anderson et al



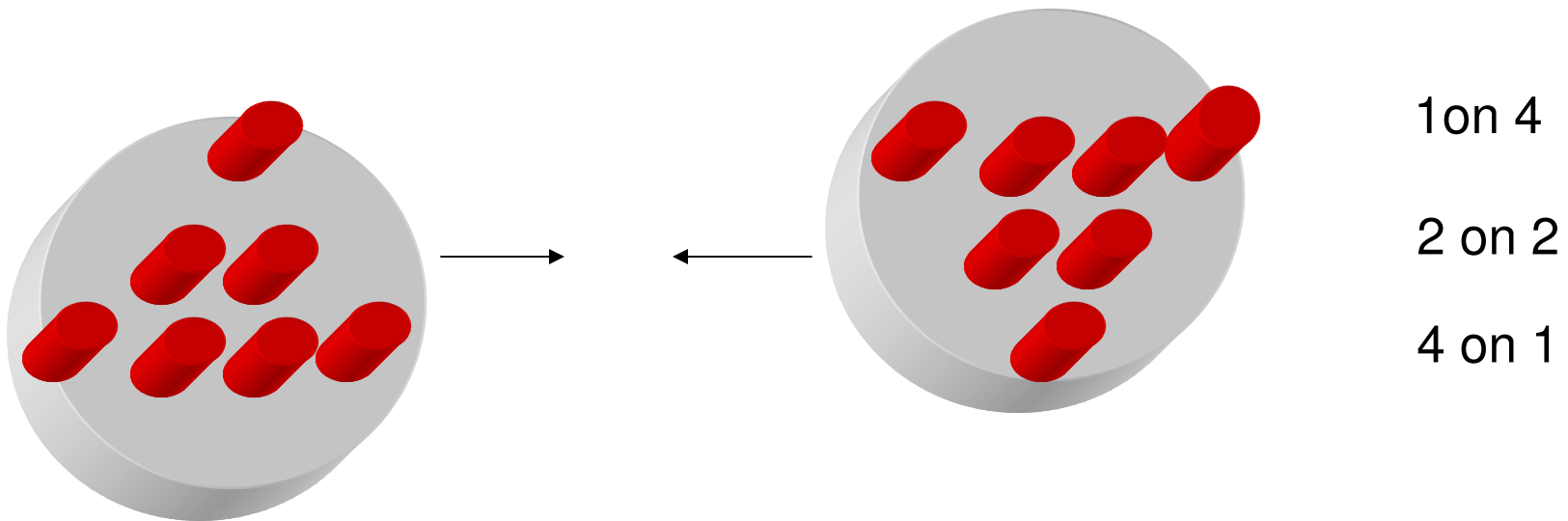
Predicted “AA Trapezoid”

$$1 \leq \frac{dN_{AA}}{A \times dN_{pp}} \leq 2$$



Key Test and controls
Initial Matter Geometry!

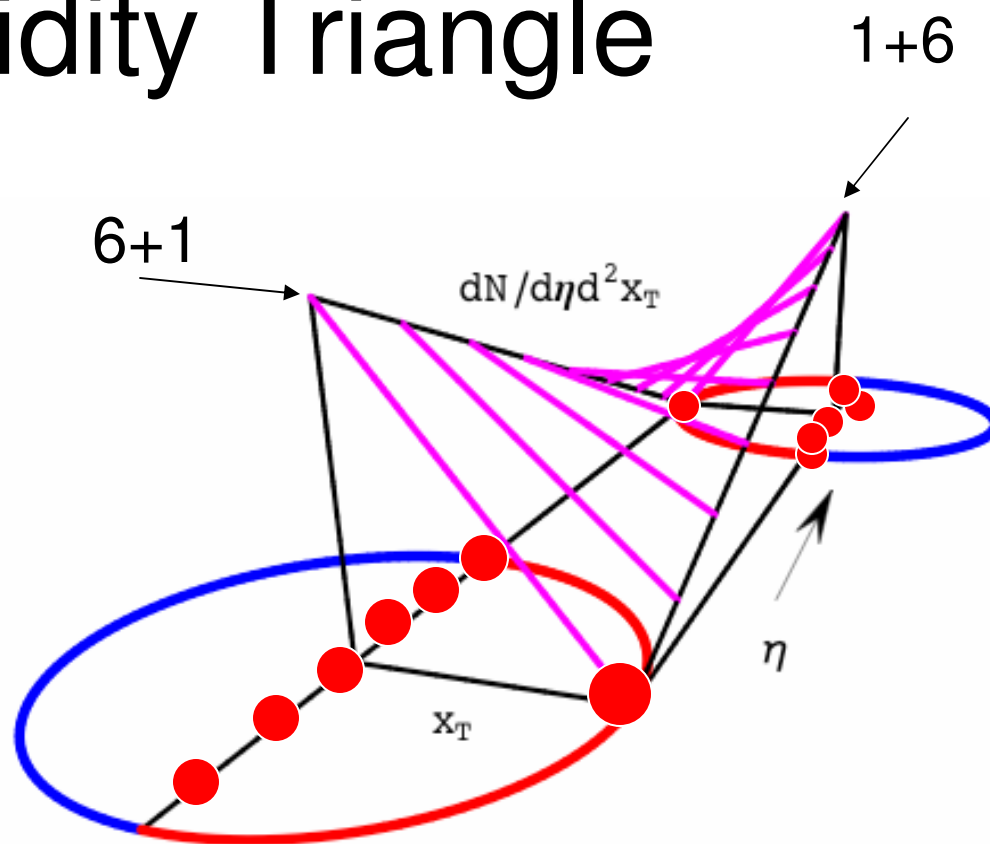
At finite impact parameter AA requires understanding pA and pp



The surface edges are controlled by equivalent p+A and intrinsically dilute physics. Need data to constrain Models of this.

Local Rapidity Triangle

- Rapidity dependent local participant density with BGK
- Note *global* multiplicity is boost invariant for $A = B$ but the local density is NOT!

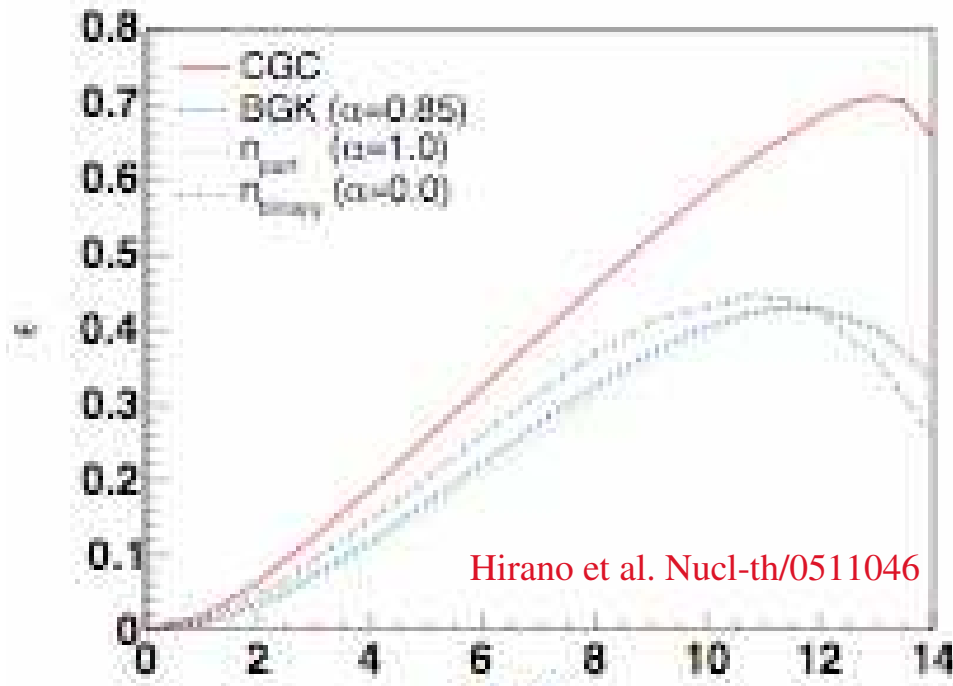


$$\rho_{Part}(\vec{x}_{\perp}) \propto e^{-\frac{y^2}{\sigma_y^2}} \left(\rho_{Part}^A \left(1 + \frac{y}{Y} \right) + \rho_{Part}^B \left(1 - \frac{y}{Y} \right) \right)$$

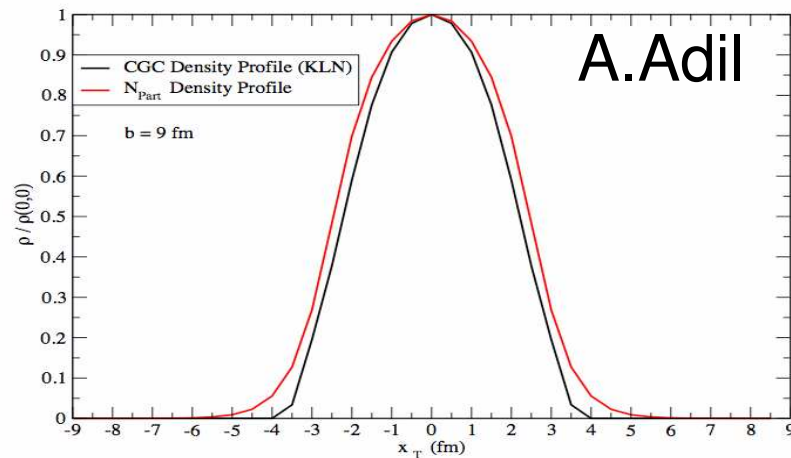
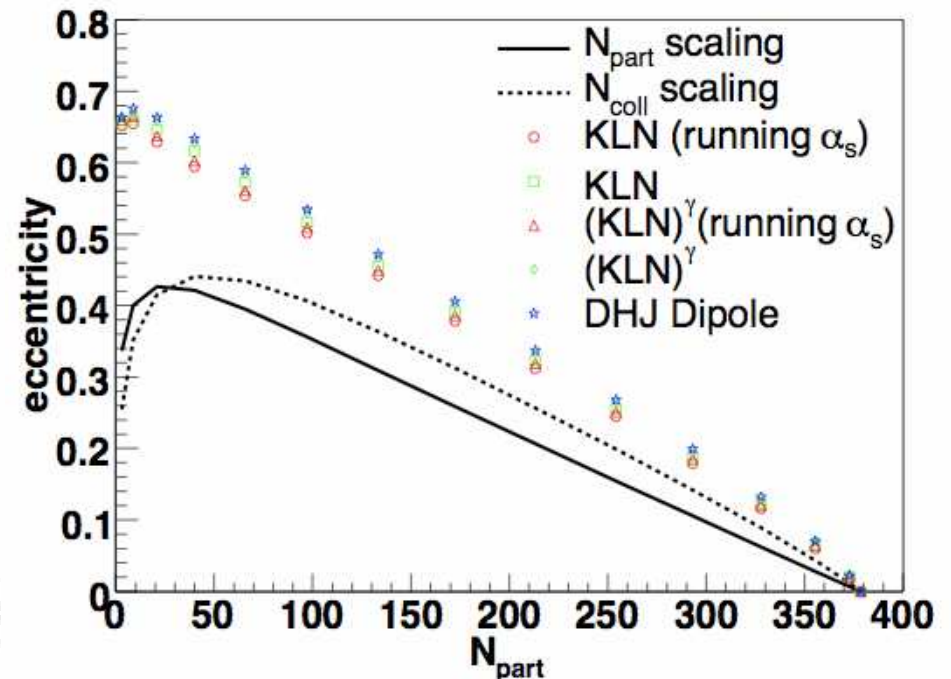
Leads to rapidity triangular edges where local physics is like p+A

CGC has sharper edges than Glauber

Leads to higher transverse space eccentricity



Hirano et al. Nucl-th/0511046



A.Adil

H.Drescher et al

More eccentric CGC leads to too
Higher elliptic anisotropic flow!
and thus

Requires viscosity to compensate

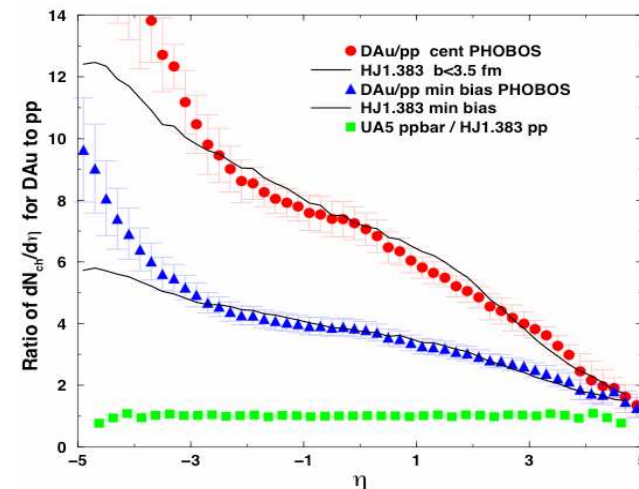
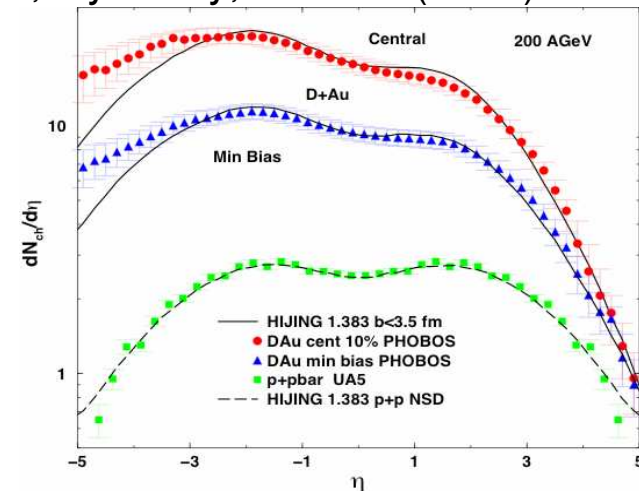
Critical Consistency test for Glauber p+A geometry

- Monte Carlo HIJING based on Glauber geometry works well
- D+Au at RHIC shows the expected rapidity triangle quantitatively.

With CGC/KLN pp and pA parameters have to be tuned independently of AA to reproduce these data !!

(Use also high p_T Tomography to further Differentiate Adil et al, Phys. Rev. D 73 (2006) 074006)

Adil, Gyulassy, PRC 72 (2005) 034907



My conclusion part III:

Current CGC/KNL model overpredicts eccentricity
And therefore elliptic flow because it incorrectly extrapolates
Central AA to the p+A and p+p edges of the reaction
Transverse plane.

Key experiment at LHC to test different models
of geometries will be the p+Pb “rapidity triangle”
and its dependence on the p_T

I predict that the correct answer will interpolate between
CGC-like geom for $Q_{\text{sat}} > 1$ GeV and Glauber like for $Q_{\text{sat}} < 1$ GeV

The im?Perfection of the sQGP fluid at LHC will only be
quantified once the initial geometry is fixed by
independent observables in pp and pPb