

# Quarkonium production in coherent $AA$ collisions and small- $x$ physics

Magno V.T. Machado

(In collaboration with Victor Gonçalves, IFM-UFPeL, Brazil)

Universidade Federal do Pampa - UNIPAMPA, Brazil

# Outline

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- Short motivation
- Ultra-Peripheral Collisions (UPCs) of heavy ions
- Quarkonium production in UPCs
- Model for photonuclear cross section - color dipole approach
- Results for exclusive  $J/\Psi$  and  $\Upsilon$  production
- Summary.

# Motivation

- UPCs are defined as collisions in which **no hadronic interactions** occur due to large spatial separation between projectile and target.
- Interactions are mediated by the **electromagnetic field**.
- One type of UPC is the **photonuclear interactions**, in which a photon from the projectile interacts with the hadronic component of target.
- **Good reasons** to study electromagnetic interactions at hadron colliders:
  - (1) Range of accessible **photon energies** will be strongly increased at the LHC and the **equivalent luminosities** will be higher than at existing electron colliders.
  - (2) Using **nuclear beams** effects of very strong fields can be studied (small- $x$  physics, nuclear shadowing, ...).

# Motivation

- Concerning **quarkonium production** in UPCs, if the **photon spectrum** is known,  $d\sigma/dy$  is a direct measure of the meson **photoproduction cross section** for a given photon energy.
- In the LHC (PbPb mode) the photon energies for production around mid-rapidity correspond to a gluon  $x$ -values of  $6 \times 10^{-4}$  for  $J/\Psi$  production and  $2 \times 10^{-3}$  for  $\Upsilon$  production. Lower values of  $x$  can be reached away from mid-rapidity.
- **Experimental feasibility** of studying exclusive meson production in UPCs has been demonstrated at **RHIC** (coherent  $\rho$  production measured by **STAR** and  $J/\Psi$  production in **PHENIX**).
- The Yellow Report of Prediction for UPCs at the LHC has been recently completed.

# UPCs of heavy ions

- The electromagnetic field of a relativistic particle corresponds to an **equivalent flux of photons**.
- In the case of interaction between **two nuclei**, in general the photon spectrum is computed as a function of **impact parameter** in a semi-classical approach.
- Thus, interactions where the nuclei interact strongly can be excluded (roughly speaking, considering  $b > 2R_A$ ).
- We consider an analytical expression for photon spectrum:

$$\frac{dn_\gamma}{dk} = \frac{2 Z^2 \alpha_{em}}{\pi k} \left[ \bar{\eta} K_0(\bar{\eta}) K_1(\bar{\eta}) + \frac{\bar{\eta}^2}{2} (K_1^2(\bar{\eta}) - K_0^2(\bar{\eta})) \right],$$

- The **photon energy** is  $k$  and  $\bar{\eta} = 2kR_A/\gamma_L$ .

# Quarkonium production in UPCs

- The total exclusive cross section for heavy mesons can be written as an integral over the equivalent photon energy:

$$\sigma(A + A \rightarrow A + A + V) = 2 \int \sigma_{\gamma+A \rightarrow V+A}(k) \frac{dn_{\gamma}}{dk} dk$$

- The **rapidity**  $y$  of the produced vector meson is related to its mass,  $M_V$ , and the photon energy through  $k = (M_V/2) \exp(y)$ .

- The rapidity distribution can be obtained as

$$\frac{d\sigma(AA \rightarrow AA + V)}{dy} = k_1 \frac{dn_{\gamma}}{dk_1} \sigma_{\gamma A \rightarrow V A}(k_1) + k_2 \frac{dn_{\gamma}}{dk} \sigma_{\gamma A \rightarrow V A}(k_2),$$

- Here,  $k_{1,2} = (M_V/2) \exp(\pm y)$ . At mid-rapidity,  $k_1 = k_2$  and the contributions from the two terms are equal.

# Photonuclear cross section

- The photonuclear cross section can be written as

$$\sigma(\gamma A \rightarrow V A) = \left. \frac{d\sigma(\gamma A \rightarrow V A)}{dt} \right|_{t=0} \int_{t_{min}}^{\infty} d|t| |F_A(t)|^2$$

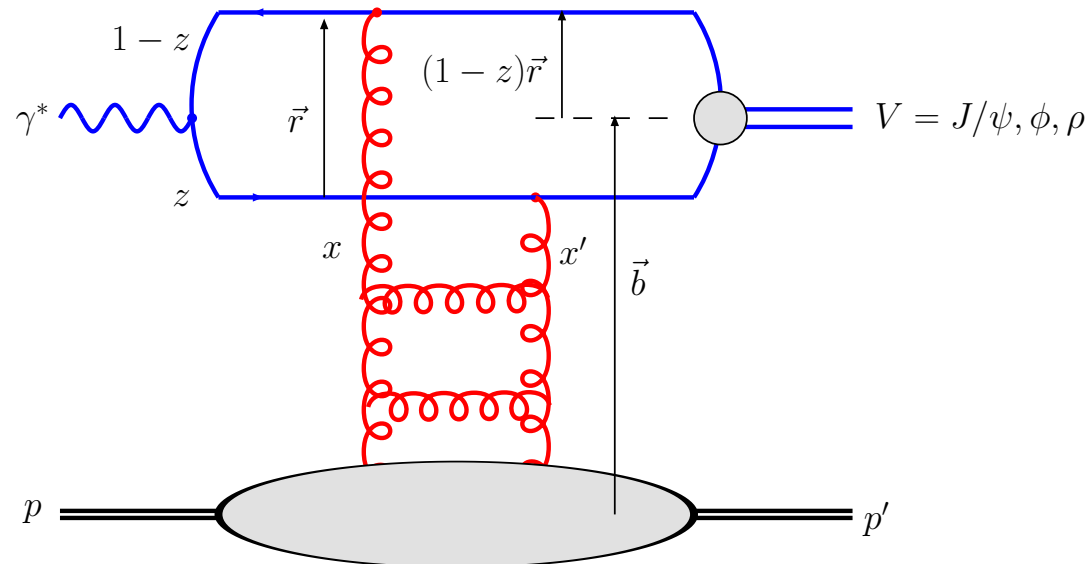
- $F_A(t)$  is the nuclear form factor and  $t_{min} = (M_V^2/4k\gamma_L)^2$ .
- Different implementations of  $\left. \frac{d\sigma(\gamma A \rightarrow V A)}{dt} \right|_{t=0}$  in literature.
- **Klein and Nystrand**: consider hadronic shadowing **negligible** for  $J/\Psi$  and  $\Upsilon$ ,  $\left. \frac{d\sigma(\gamma A \rightarrow V A)}{dt} \right|_{t=0} = A^2 \left. \frac{d\sigma(\gamma p \rightarrow V p)}{dt} \right|_{t=0}$ . Last quantity is taken from a fit to HERA data for vector mesons (and its corresponding extrapolation).
- **M. Strikman and collaborators**: consider leading twist shadowing  $\left. \frac{d\sigma(\gamma A \rightarrow V A)}{dt} \right|_{t=0} = \frac{[xg_A(x, \bar{Q})]^2}{[xg_N(x, Q)]^2} \left. \frac{d\sigma(\gamma p \rightarrow V p)}{dt} \right|_{t=0}$ . Last quantity also taken from fits to HERA data.

# Model for photonuclear reaction

- We consider the color dipole approach to compute the photonuclear cross section (valid for  $x \lesssim 10^{-2}$ ).

$$\mathcal{A}(\gamma A \rightarrow V A) = -i \int dz d^2\mathbf{r} \Psi_V^*(z, \mathbf{r}) \sigma_{dip}^{\text{nuc}}(x, \mathbf{r}; A) \Psi_\gamma(z, \mathbf{r}, Q^2)$$

- The basic quantities are the photon and vector meson wavefunction ( $\Psi_\gamma$  and  $\Psi_V$ ) as well as the dipole-target cross section,  $\sigma_{dip}^{\text{nuc}}(x, \mathbf{r}; A)$ .





# Meson wave function

- We consider the simple Gaus-LC wave functions, which are shown to reproduce DESY-HERA data for vector meson photoproduction and electroproduction.
- Small sensitivity to a different choice for the meson wave function (for instance, boosted Gaussian) in photoproduction.
- The parameters of meson wave functions are determined by requiring the normalization condition and decay width.
- Photon wave functions are known.

# Dipole-nucleus cross section

- Dipole-target cross section can be extended for nuclear case using the [Glauber-Gribov picture](#):

$$\sigma_{dip}^{\text{nuc}}(x, r; A) = 2 \int d^2b \left\{ 1 - \exp \left[ -\frac{1}{2} A T_A(b) \sigma_{dip}(x, r) \right] \right\}$$

- Nuclear profile function  $T_A(b)$  (from Wood-Saxon), where  $b$  is the impact parameter of the center of the dipole relative to the center of the nucleus.
- It sums up all the **multiple elastic rescattering diagrams** of the  $q\bar{q}$  pair and is justified for large coherence length.
- Approach describes (scarce) data for the nuclear ratios for  $x \leq 10^{-2}$  (for instance, see Armesto, EPJC26 (2002) 35).
- The main input is the dipole-proton cross section,  $\sigma_{dip}(x, r)$ .

# Dipole-proton cross section

- We take recent parameterization based on the saturation physics [Iancu-Itakura-Munier, PLB590:199, 2004]:

$$\sigma_{dip}^{CGC}(x, r) = \sigma_0 \begin{cases} \mathcal{N}_0 \left( \frac{\bar{r}^2}{4} \right)^{\gamma_{\text{eff}}(x, r)}, & \text{for } \bar{r} \leq 2, \\ 1 - \exp \left[ -a \ln^2(b \bar{r}) \right], & \text{for } \bar{r} > 2, \end{cases}$$

where  $\bar{r} = r Q_{\text{sat}}$  and  $\gamma_{\text{eff}}(x, r) = \gamma_{\text{sat}} + \frac{\ln(2/\bar{r})}{\kappa \lambda Y}$ , where  $\gamma_{\text{sat}} = 0.63$ ,  $\kappa = 9$  and  $Y = \ln(1/x)$ .

- **Saturation scale** is given by  $Q_{\text{sat}} = (x_0/x)^{\lambda/2}$ .
- Most recent fit to small- $x$  HERA data:  $x_0 = 2.7 \times 10^{-7}$ ,  $\lambda = 0.177$  and  $\sigma_0 = 35.7 \text{ mb}$  ( $\chi^2/\text{dof} = 0.9$  for  $Q^2 = [0.5, 45]$ ).
- Ref.: Kowalski, Motyka and Watt, PRD74: 074016 (2006).
- Quark masses are  $m_q = 0.14 \text{ GeV}$  and  $m_c = 1.4 \text{ GeV}$ .

# Corrections for exclusive processes

- The **real part of amplitude** can be accounted for by multiplying the differential cross section by a factor  $(1 + \beta^2)$ .
- The ratio of real to imaginary parts is given by:

$$\beta = \tan\left(\frac{\pi\alpha}{2}\right), \quad \text{where } \alpha \equiv \frac{\partial \ln [\mathcal{A}(\gamma A \rightarrow V A)]}{\partial \ln(W^2)}$$

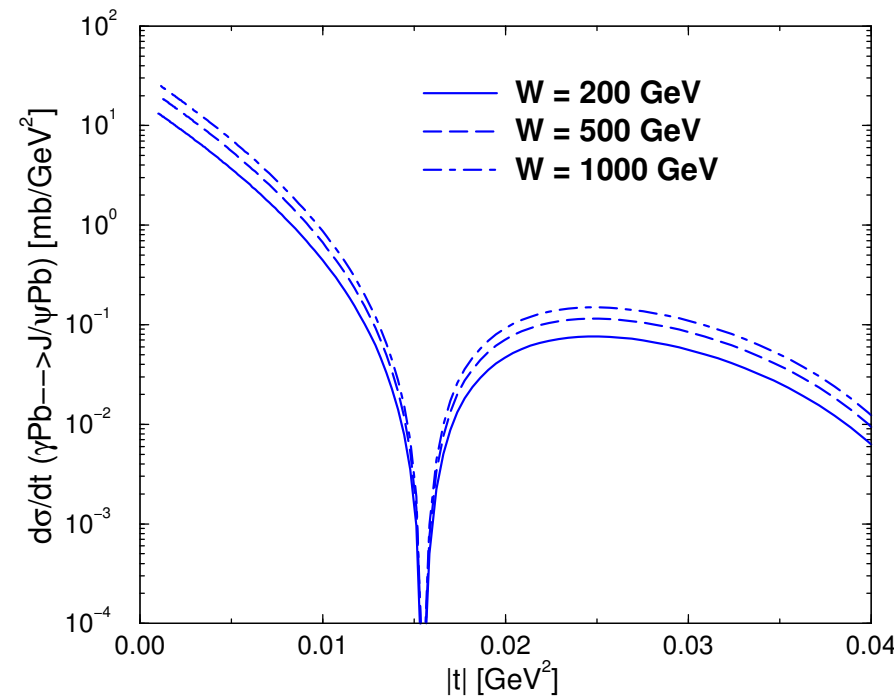
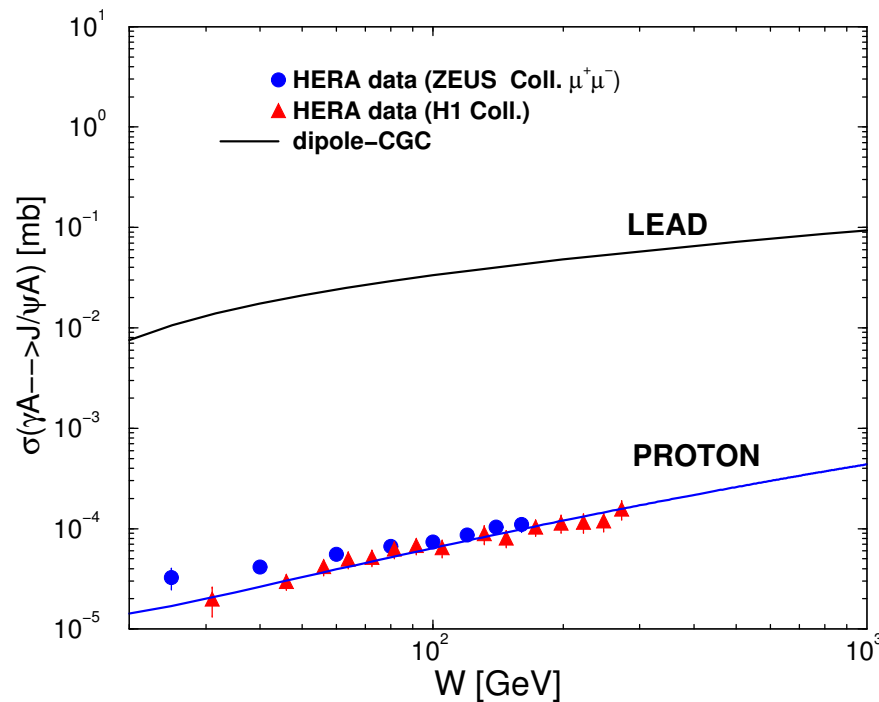
- For exclusive production, **off-diagonal gluon distribution** should be used, since the two exchanged gluons carry different fractions  $x$  and  $x'$  of the proton's momentum.
- Off-forward effects can be (phenomenologically) accounted for by multiplying the differential cross section by a factor  $R_g^2$  [Shuvaev et al., **Phys. Rev D60 014015 (1999)**], where

$$R_g = \frac{2^{2\alpha+3}}{\sqrt{\pi}} \frac{\Gamma\left(\alpha + \frac{5}{2}\right)}{\Gamma(\alpha + 4)}$$

# Numerical results - $J/\Psi(1S)$

Photoproduction of  $V = J/\Psi(3097)$ :

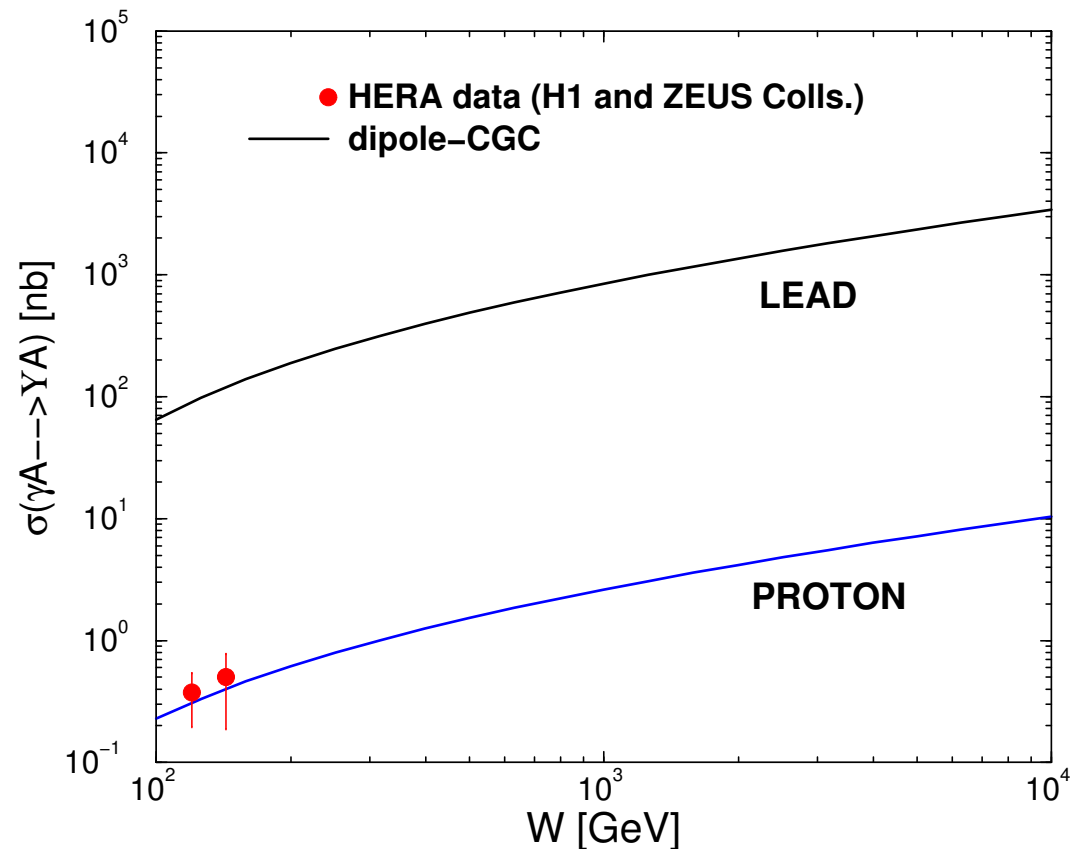
- Photonuclear cross section as a function of  $W_{\gamma A}$ .
- Extrapolation to  $W_{\gamma A} = 1$  TeV.
- Differential cross section as a function of  $|t|$ .



# Numerical results - $\Upsilon(1S)$

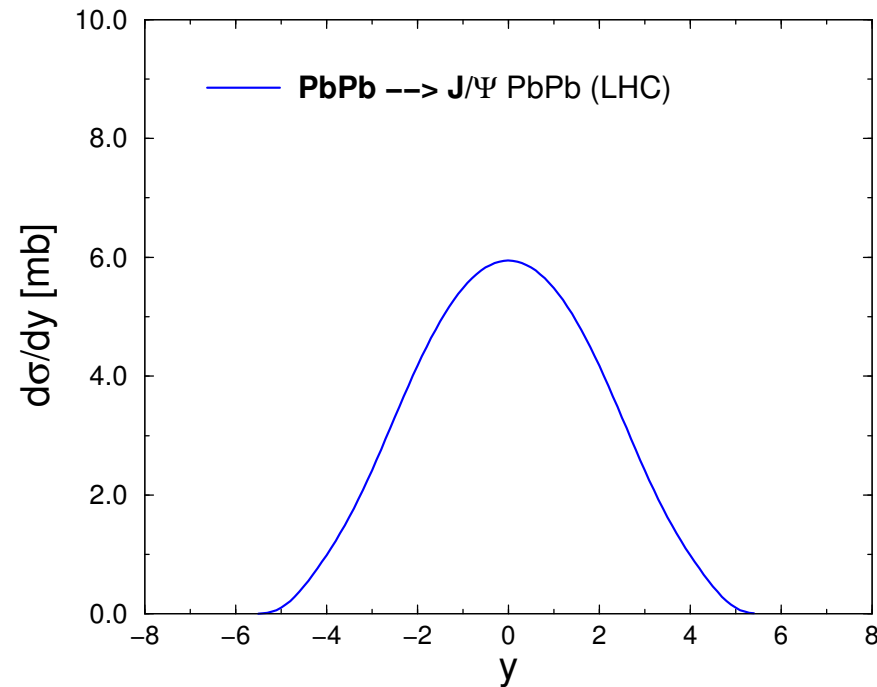
Photoproduction of  $V = \Upsilon(1S)$ :

- Photonuclear cross section as a function of  $W_{\gamma A}$ .
- Comparison with the (scarse) DESY-HERA data.
- We use bottom mass  $m_b = 4.2$  GeV.



# Photoproduction in $AA$ collisions

## $J/\Psi$ photoproduction in $AA$ collisions

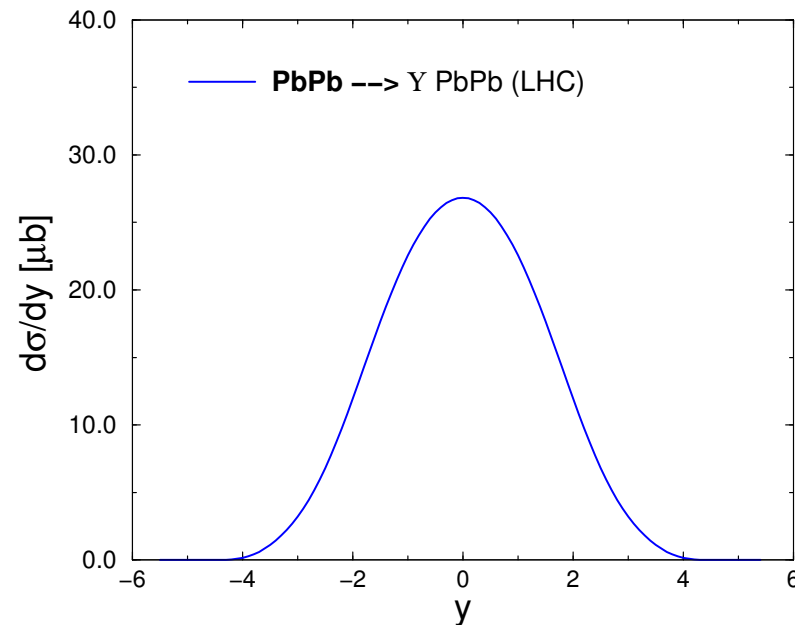


● Integrated cross section at the LHC:  $\frac{d\sigma(y=0)}{dy} = 6 \text{ mb}$ .

$y$ -cut	this work	FS	KN	hadropr. [ $A^2 \times \sigma(pp)$ ]
total	32 mb	15 mb	32 mb	820 mb
$ y  < 1$	11 mb	—	—	—

# Photoproduction in $AA$ collisions

## $\Upsilon$ photoproduction in $AA$ collisions



- Integrated cross section at the LHC:  $\frac{d\sigma(y=0)}{dy} = 27 \mu\text{b}$ .

$y$ -cut	this work	FS	KN	hadropr. [ $A^2 \times \sigma(pp)$ ]
total	96 $\mu\text{b}$	78 $\mu\text{b}$	170 $\mu\text{b}$	8 mb
$ y  < 1$	48 $\mu\text{b}$	—	—	—



# Comments and remarks

- In the  $pA$  collisions the quasireal photons can be emitted by both the nucleus and the proton.
- The expression for the cross section takes the form

$$\frac{d\sigma(pA \rightarrow pA + V)}{dydt} = \frac{dn_{\gamma}^A}{dk_1} \frac{\sigma_{\gamma p \rightarrow Vp}(y)}{dt} + \frac{dn_{\gamma}^p}{dk_2} \frac{\sigma_{\gamma A \rightarrow VA}(-y)}{dt},$$

- $\frac{dn_{\gamma}^p}{dk_2}$  is the photon flux of the accelerated proton.
- Allow to do phenomenology for  $\gamma p$  and  $\gamma A$  interactions.
- Finally, a background to the coherent production is the incoherent interaction, where the final state nucleus is excited,  $\gamma A \rightarrow V A'$ .

# Summary

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- We compute the coherent quarkonium ( $J/\Psi$  and  $\Upsilon$ ) production in UPCs for PbPb scattering at the LHC.
- For the photonuclear cross section we consider the color dipole approach, with a phenomenological model for the dipole cross section.
- The results are compatible with other phenomenological approaches in literature.
- An extension for  $pA$  collisions and an estimation of incoherent production remain to be done.